



May 23, 2019
Sao Tome und Principe

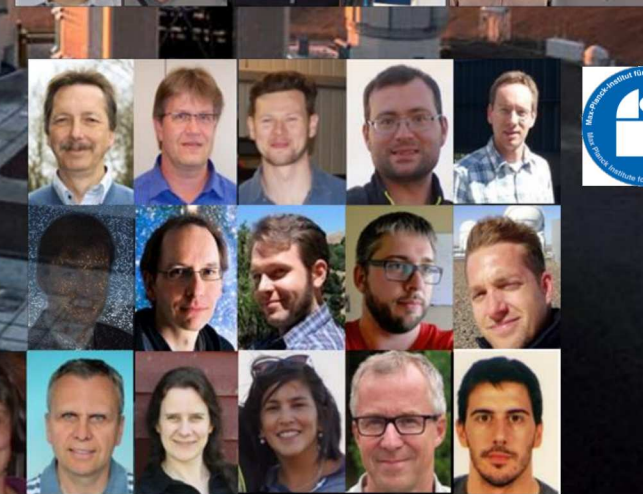
Testing General Relativity in the Galactic Center

GRAVITY Collaboration

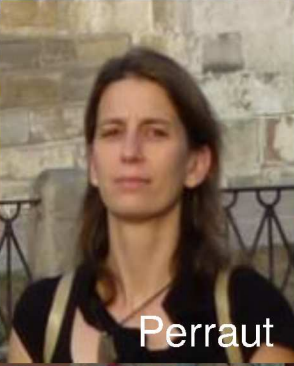
R. Abuter, A. Amorim, N. Anugu, M. Bauböck, M. Benisty, J.P. Berger, N. Blind, H. Bonnet, W. Brandner, A. Buron, C. Collin, F. Chapron, Y. Clénet, V. Coudé du Foresto, P.T. de Zeeuw, C. Deen, F. Delplancke-Ströbele, R. Dembet, J. Dexter, G. Duvert, A. Eckart, F. Eisenhauer, G. Finger, N.M. Förster Schreiber, P. Fedou, P. Garcia, R. García Lopez, F. Gao, E. Gendron, R. Genzel, S. Gillessen, P. Gordo, M. Habibi, X. Haubois, M. Haug, F. Haußmann, Th. Henning, S. Hippler, M. Horrobin, Z. Hubert, N. Hubin, A. Jimenez Rosales, L. Jochum, L. Jocou, A. Kaufer, S. Kellner, S. Kendrew, P. Kervella, Y. Kok, M. Kulas, S. Lacour, V. Lapeyrère, B. Lazareff, J.-B. Le Bouquin, P. Léna, M. Lippa, R. Lenzen, A. Mérand, E. Müller, U. Neumann, T. Ott, L. Palanca, T. Paumard, L. Pasquini, K. Perraut, G. Perrin, O. Pfuhl, P.M. Plewa, S. Rabien, J. Ramos, A. Ramírez, C. Rau, G. Rodríguez Coira, R.-R. Rohloff, G. Rousset, B. J. Sanchez-Bermudez, S. Scheithauer, M. Schöller, N. Schuler, J. Spyromilio, O. Straub, C. Straubmeier, E. Sturm, L.J. Tacconi, K.R.W. Tristram, F. Vincent, S. von Fellenberg, C. I. Wank, I. Waisberg, F. Widmann, E. Wieprecht, M. Wiest, E. Wiezorrek, J. Woillez, S. Yazici, D. Ziegler, and G. Zins



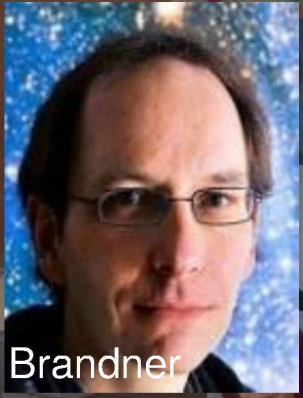
GRAVITY Collaboration



l'Observatoire
de Paris



Perraut



Brandner



Garcia



Straubmeier



Dexter



Pfuhl



Paumard



Genzel



Eckart



Gillesen



Woillez



Lacour



Perrin



Bonnet



de Zeeuw

General Relativistic Effects Around the Galactic Center Black Hole



Gravitational Effects Around the Central Black Hole

**Region of Space
Time Locked away
from Outside World**

1. *Die Grundlage
der allgemeinen Relativitätstheorie;
von A. Einstein.*

General Relativistic Effects Around the Galactic Center Black

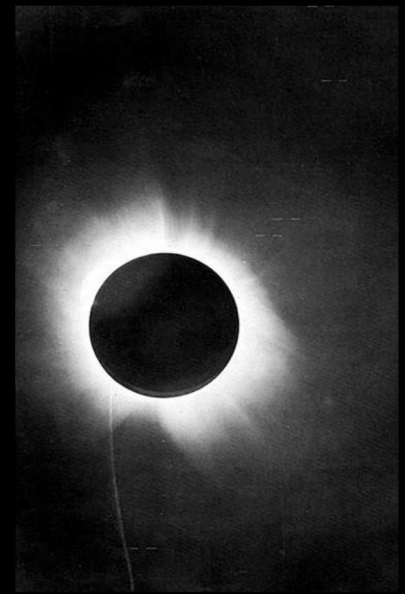
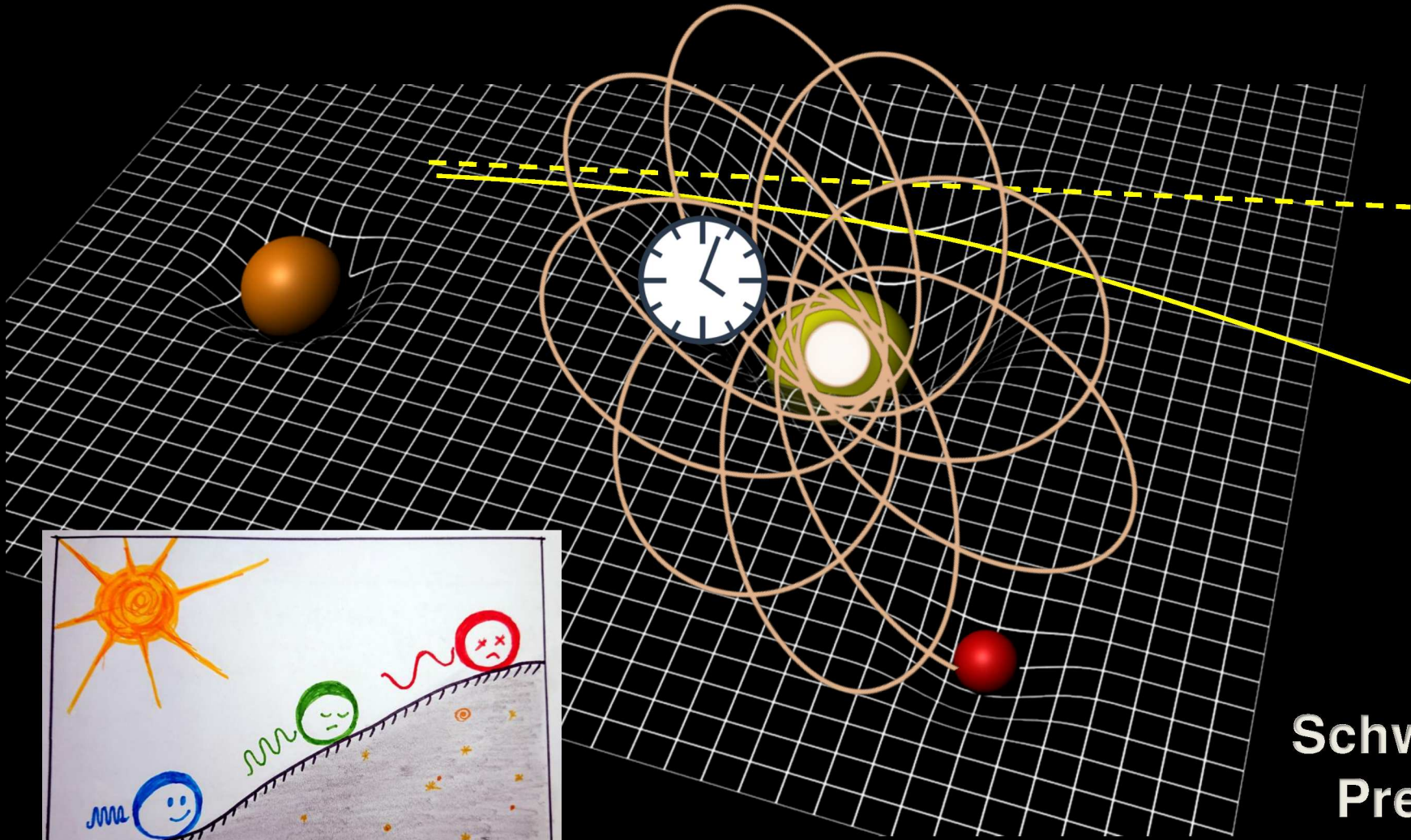


Einstein

Erklärung, welche pro vom Betrage

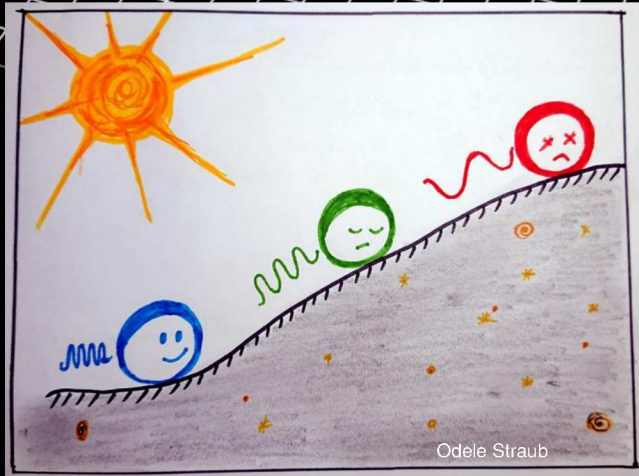
$$\varepsilon = 24 \pi^3 \frac{\alpha^2}{T^2 c^2 (1 - e^2)} \dots (25)$$

pro Umlauf. In dieser Formel bedeutet α die grosse Halbachse,
die Lichtgeschwindigkeit c und T die Umlaufzeit.



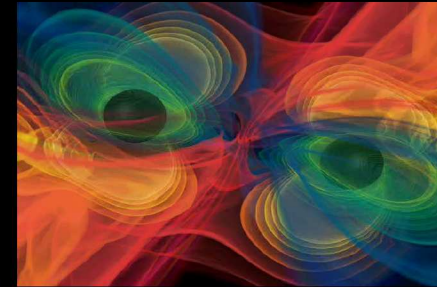
**Light
Bending**

**Schwarzschild
Precession**

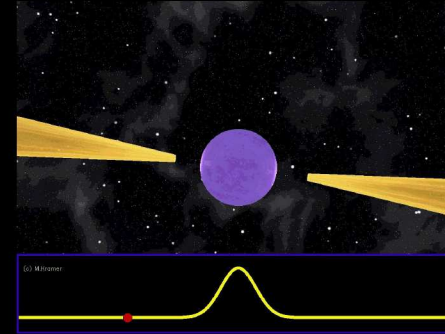
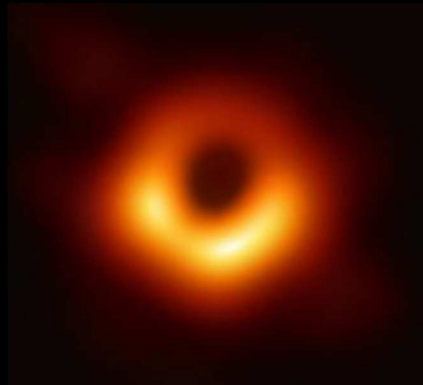


Gravitational Redshift

Talks by Alessandra and Ulrich



Talk by Carlos



Gravitational
Waves

Quadrupole
Moment

Shadow

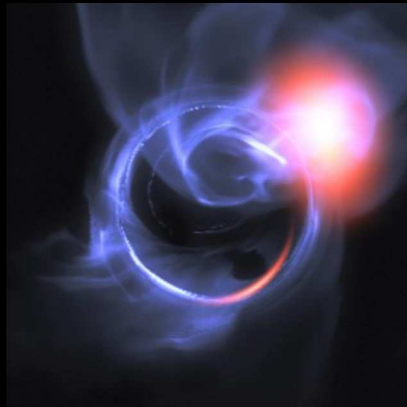
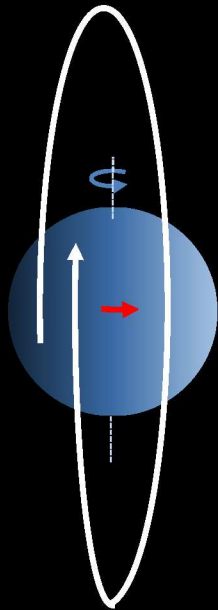
Last
Stable
Orbit

Spin

Precession

Lensing

Redshift





General Relativistic Effects Around the Galactic Center Black Hole

GRAVITY collaboration+18a,b,19, Genzel,Eisenhauer&Gillessen10, Morris,Meyer&Ghez12, Falcke&Markoff13
Eckart&Genzel96, Genzel+97,03, Ghez+98,05,08, Schödel+02, Eisenhauer+03,05, Gillessen+09,17, Paumard+07, Do+09, Meyer+12, Boehle+16, Fritz+16, Witzel+18, ...

Courtesy: ESO / MPE

Black Holes – The Quest for Hard Numbers

Is General Relativity the correct theory ?

5%

0.3%

Is the mass concentrated within the Schwarzschild radius ?

A geometric distance measurement to the Galactic Center black hole with 0.3% uncertainty

arXiv:1904.05721

Test of Einstein Equivalence Principle near the Galactic Center Massive Black Hole

Physical Review Letters, 122, 1102

3-5 R_S

Detection of Orbital Motions Near the Last Stable Circular Orbit of the Massive Black Hole SgrA*

Astronomy & Astrophysics, 618, 10

Detection of the gravitational redshift in the orbit of the star S2 near the Galactic centre massive black hole

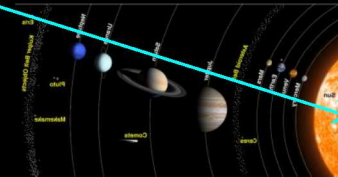
20 σ

Astronomy & Astrophysics, 615, 15

Exquisite Imaging & Astrometry

120 Astronomical Units
1400 R_s

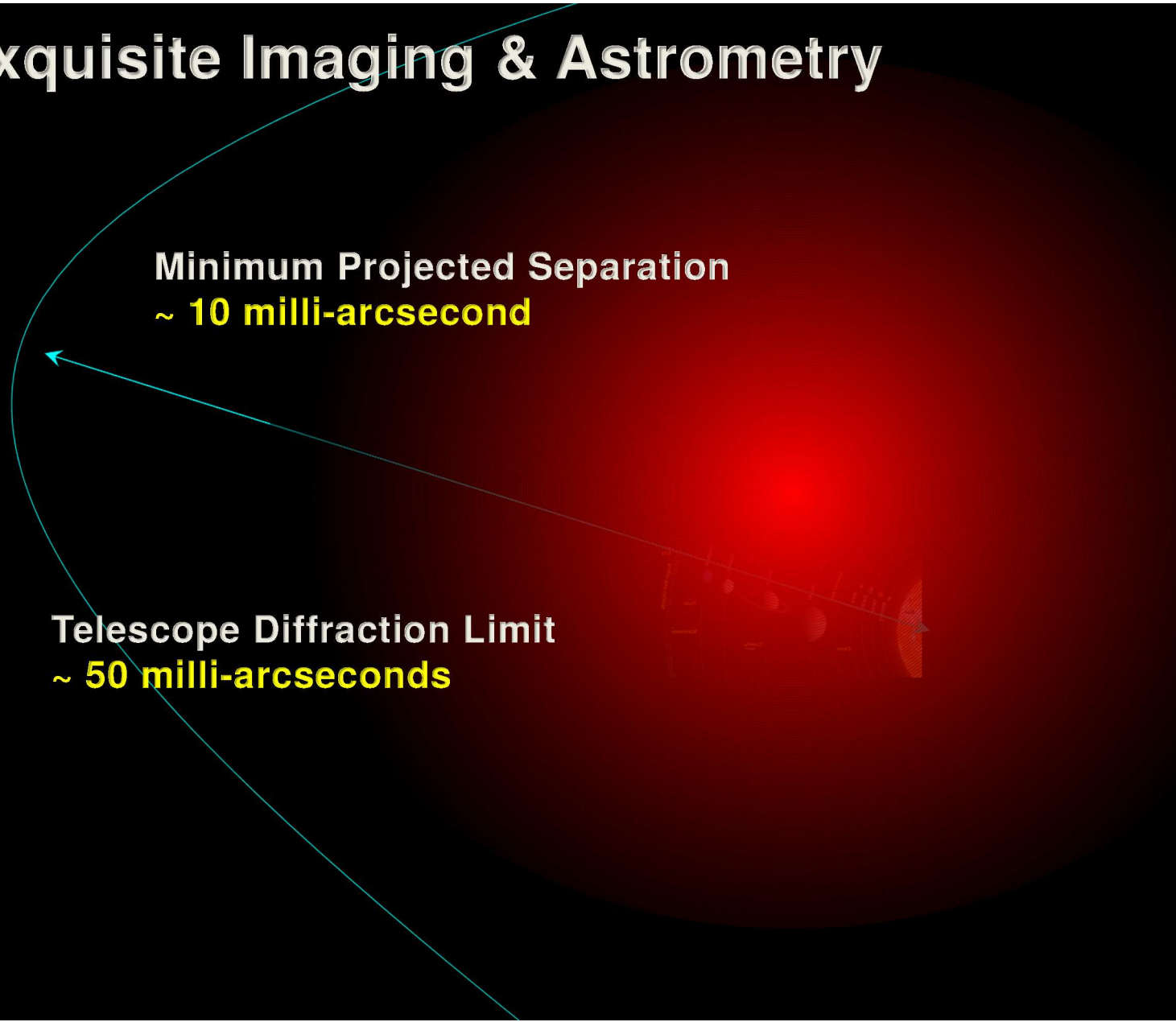
8000 km/s
2.5% Speed of Light



Exquisite Imaging & Astrometry

Minimum Projected Separation
~ 10 milli-arcsecond

Telescope Diffraction Limit
~ 50 milli-arcseconds

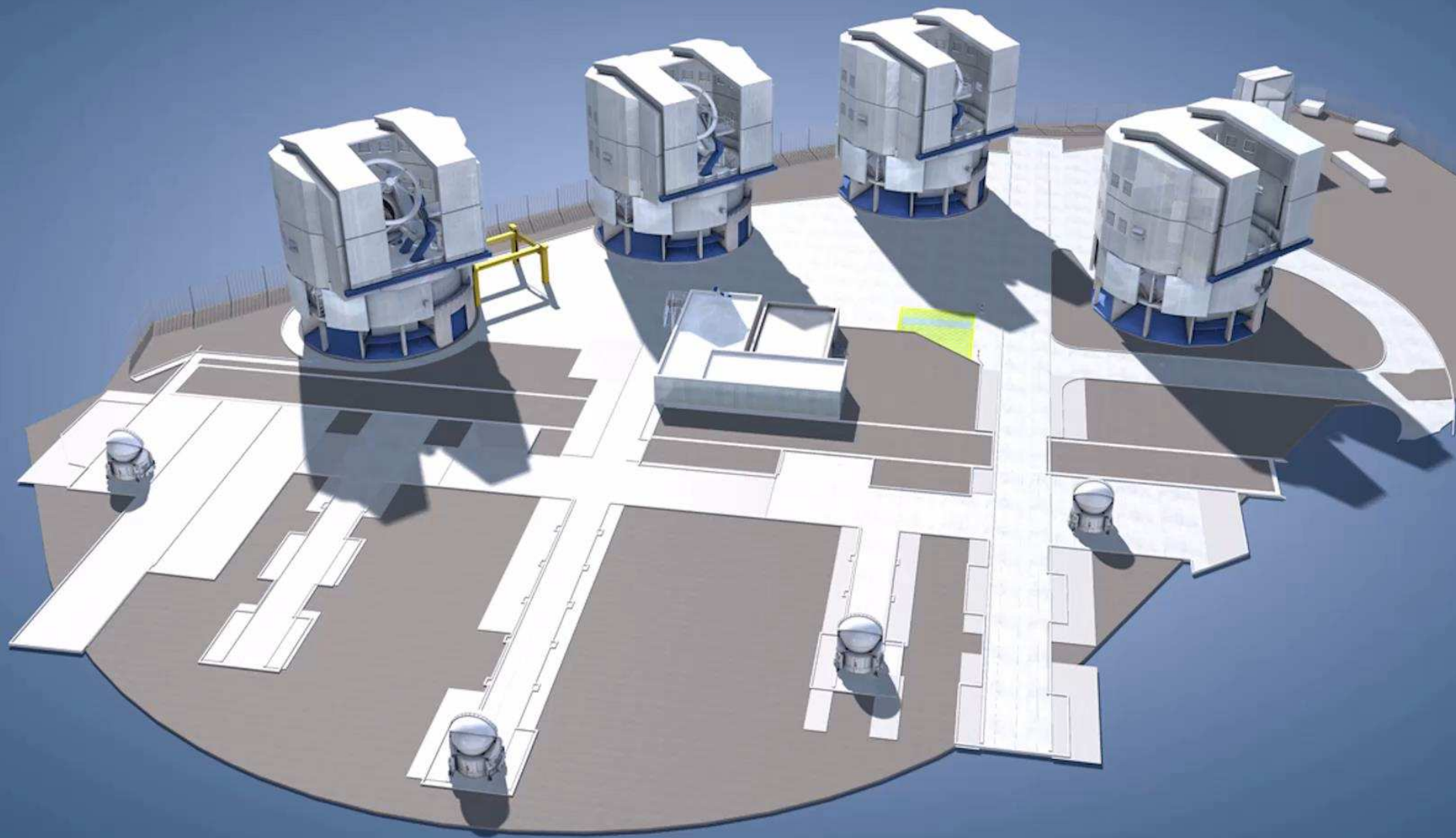


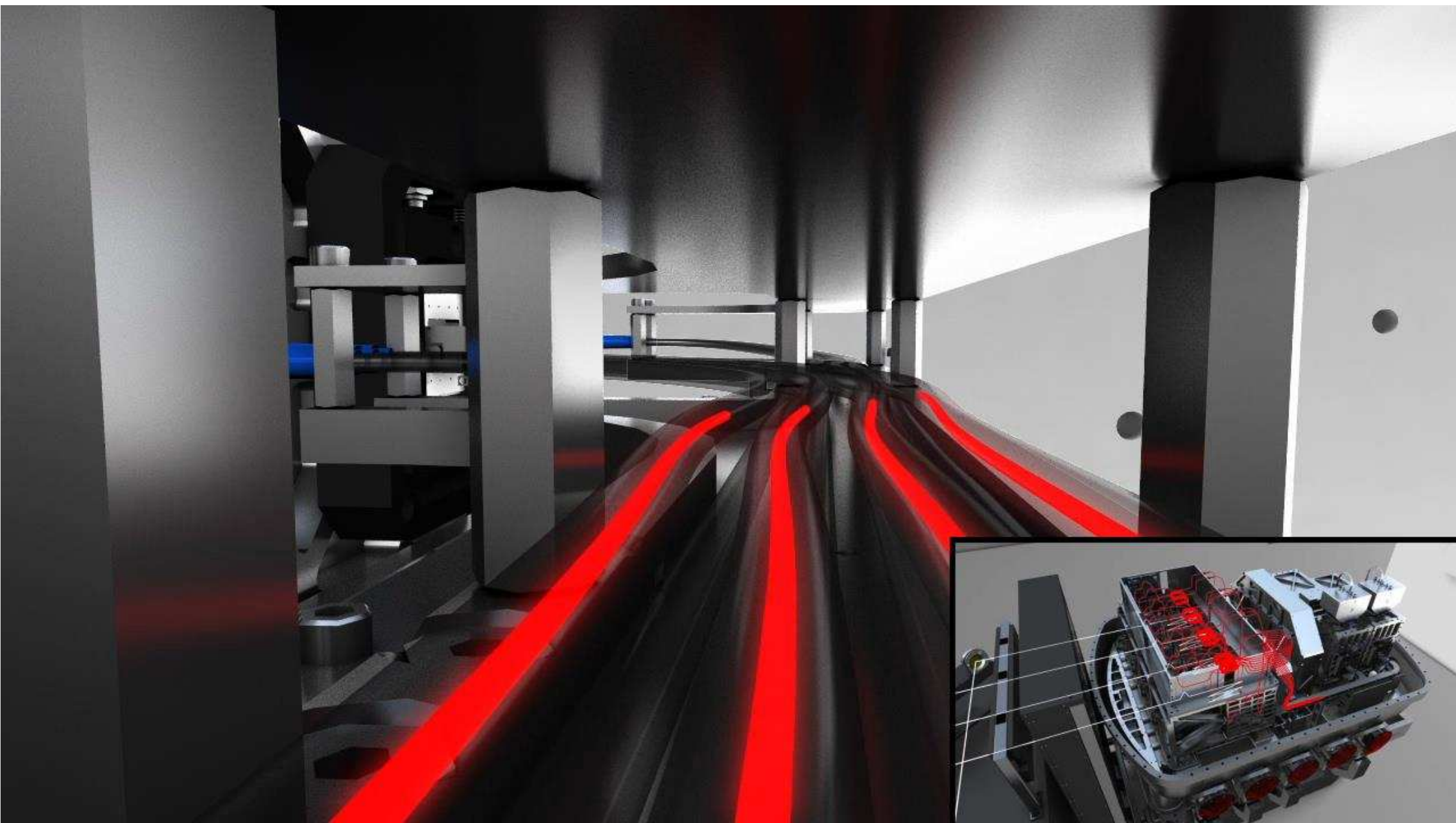


Combining the ESO VLT to a 200m Super Telescope



ESO / GRAVITY collaboration





Routine Faint Milli-Arcsec Imaging 1000x More Sensitive than Earlier Interferometer

Typically
2 hours
on source

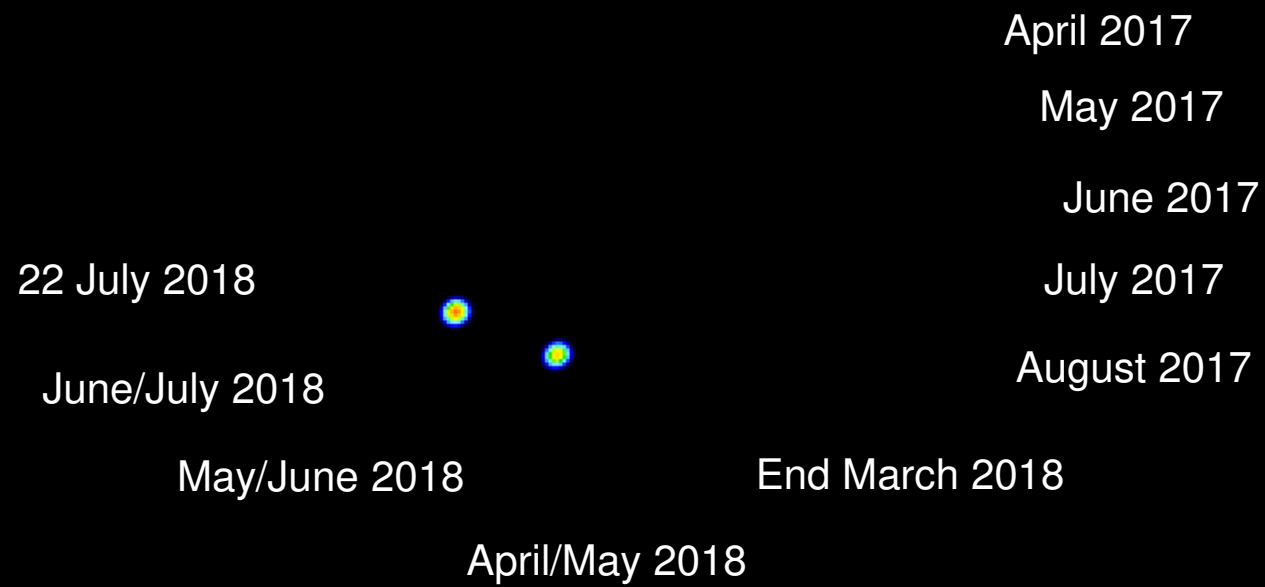


RMS noise
>20 mag

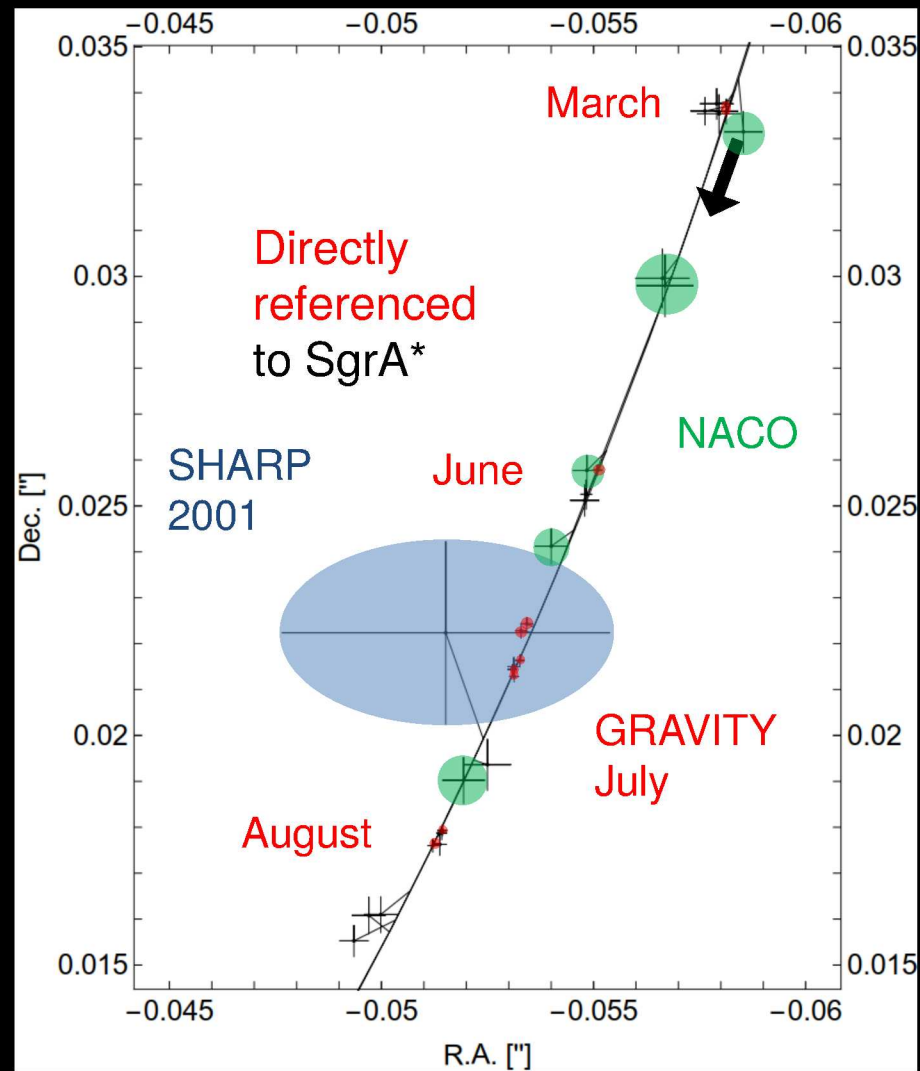
May/June 2018



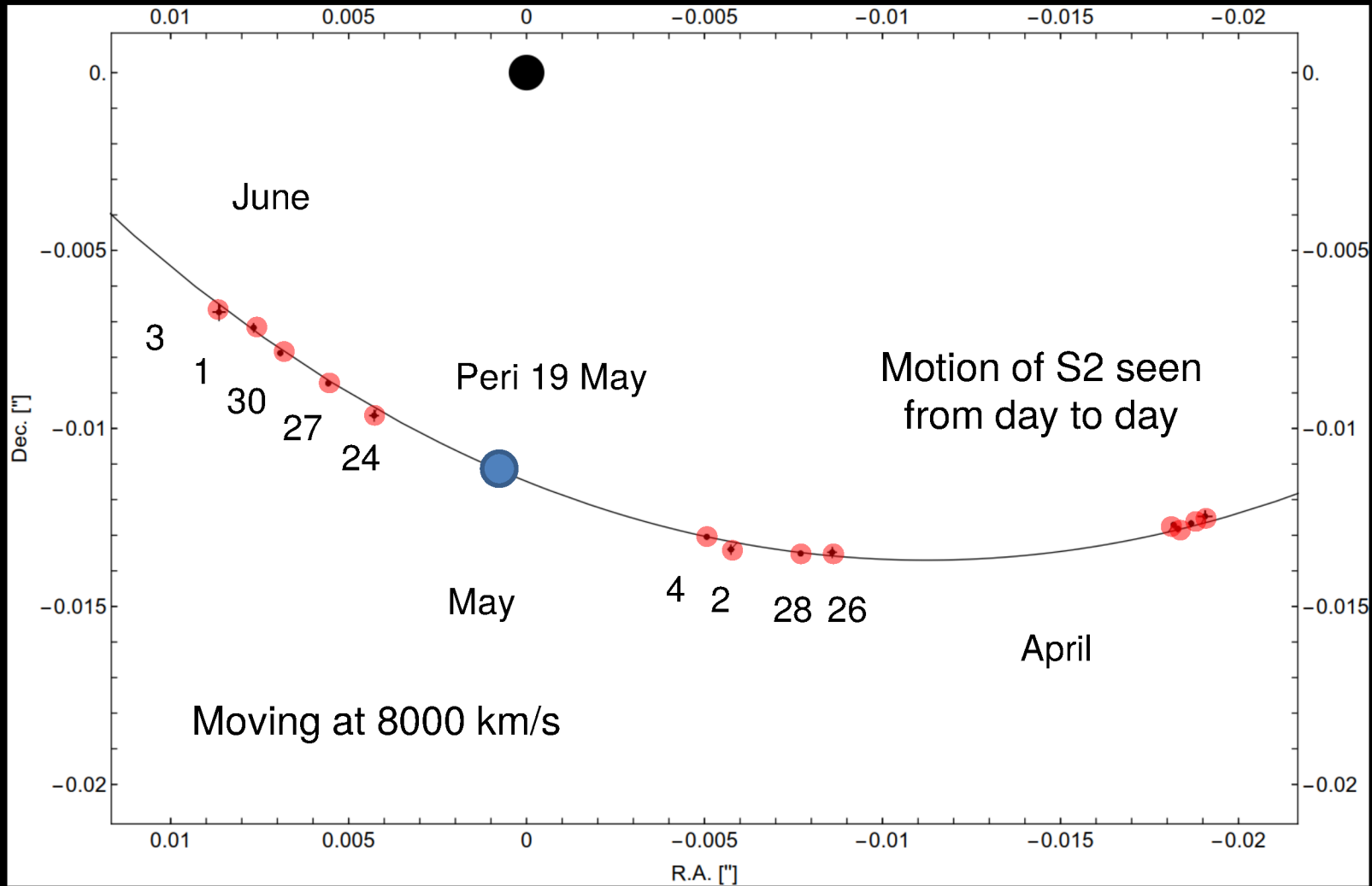
50 mas



20 – 100 Micro-Arcsecond Precision Astrometry



20 – 100 Micro-Arcsecond Precision Astrometry



Precise Mass and Distance of the Galactic Center Black Hole

Motion on sky (“arcsec/yr”) ~ Mass / Distance

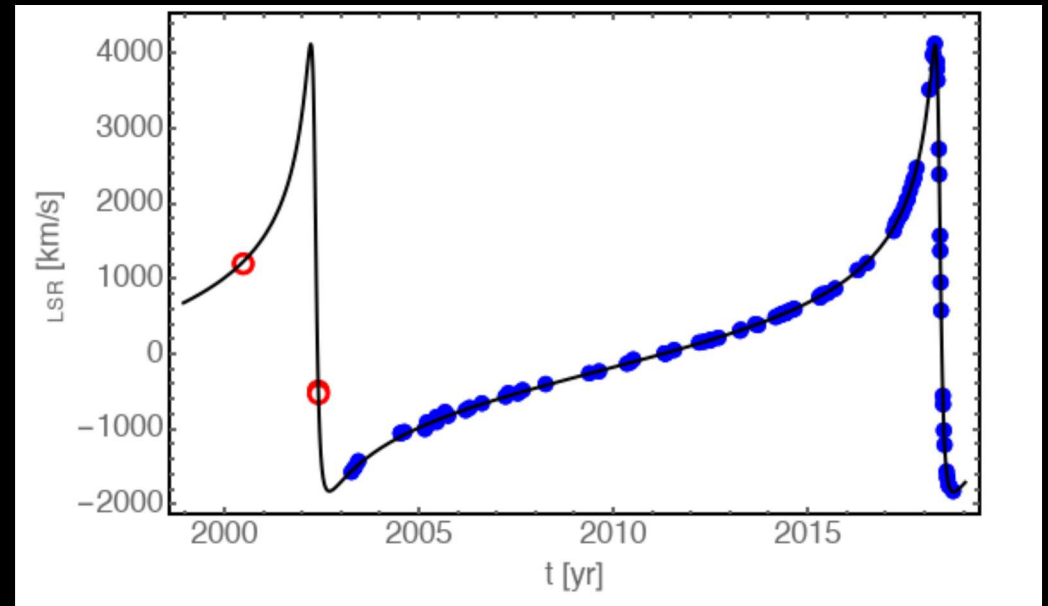
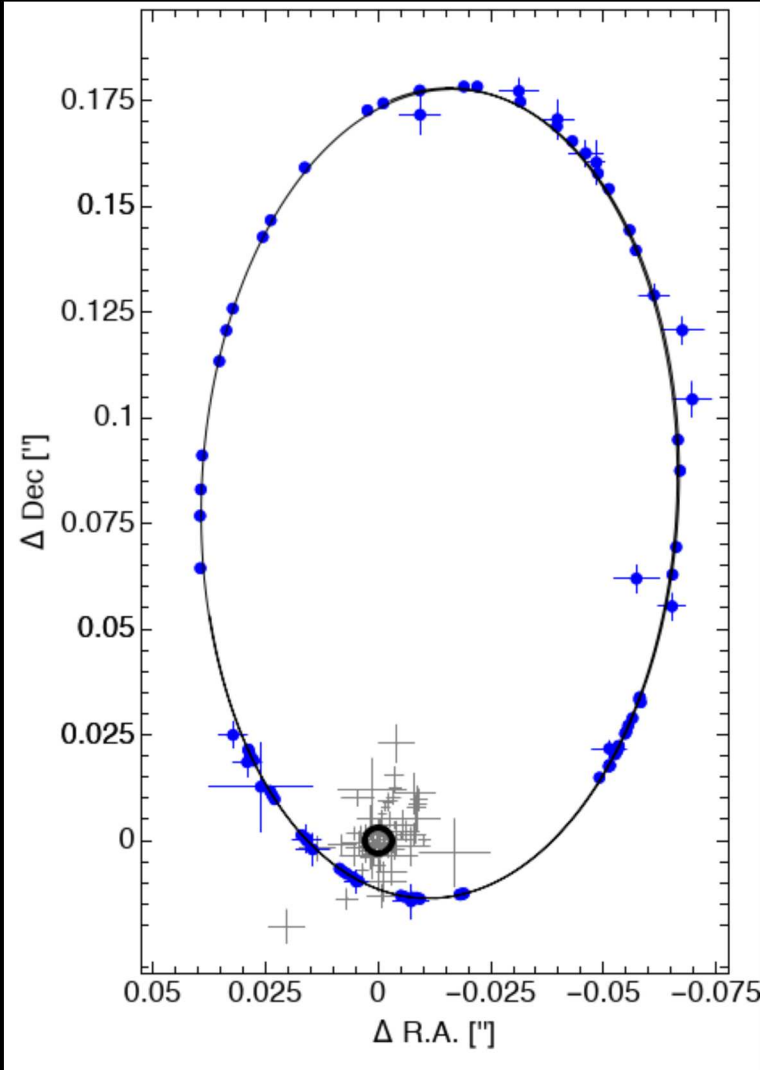
$$R_0 = 26673 \pm 42_{\text{stat}} \pm 71_{\text{sys}} \text{ ly}$$

0.33%

$$M = 4.152 \times 10^6 M_{\text{Sun}}$$

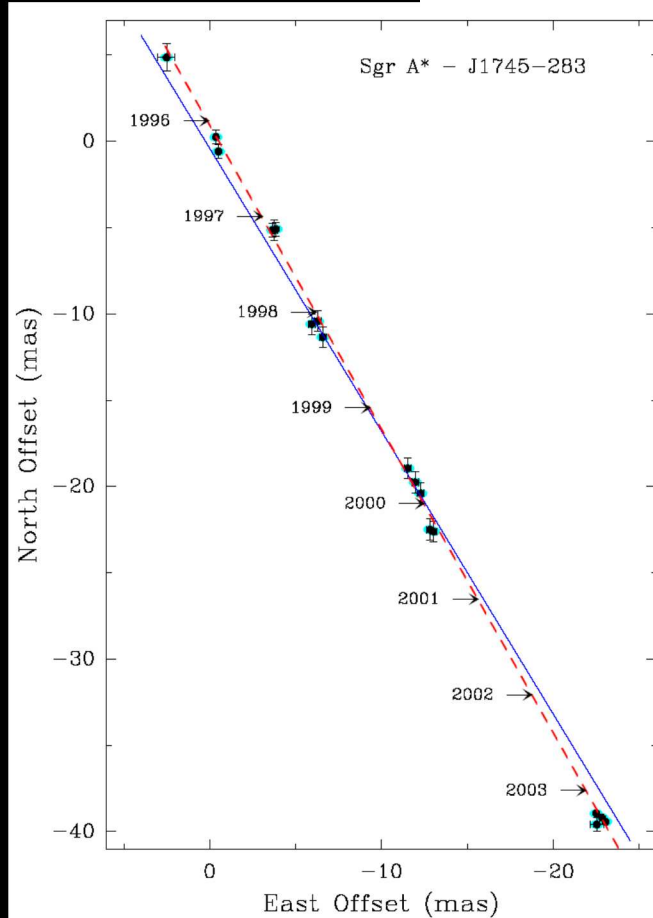
$$R_S/R_0 = 10022 \pm 20_{\text{stat}} \pm 32_{\text{sys}} \text{ Nano arcsec}$$

Radial velocity (“km/s”) ~ Mass, NOT Distance

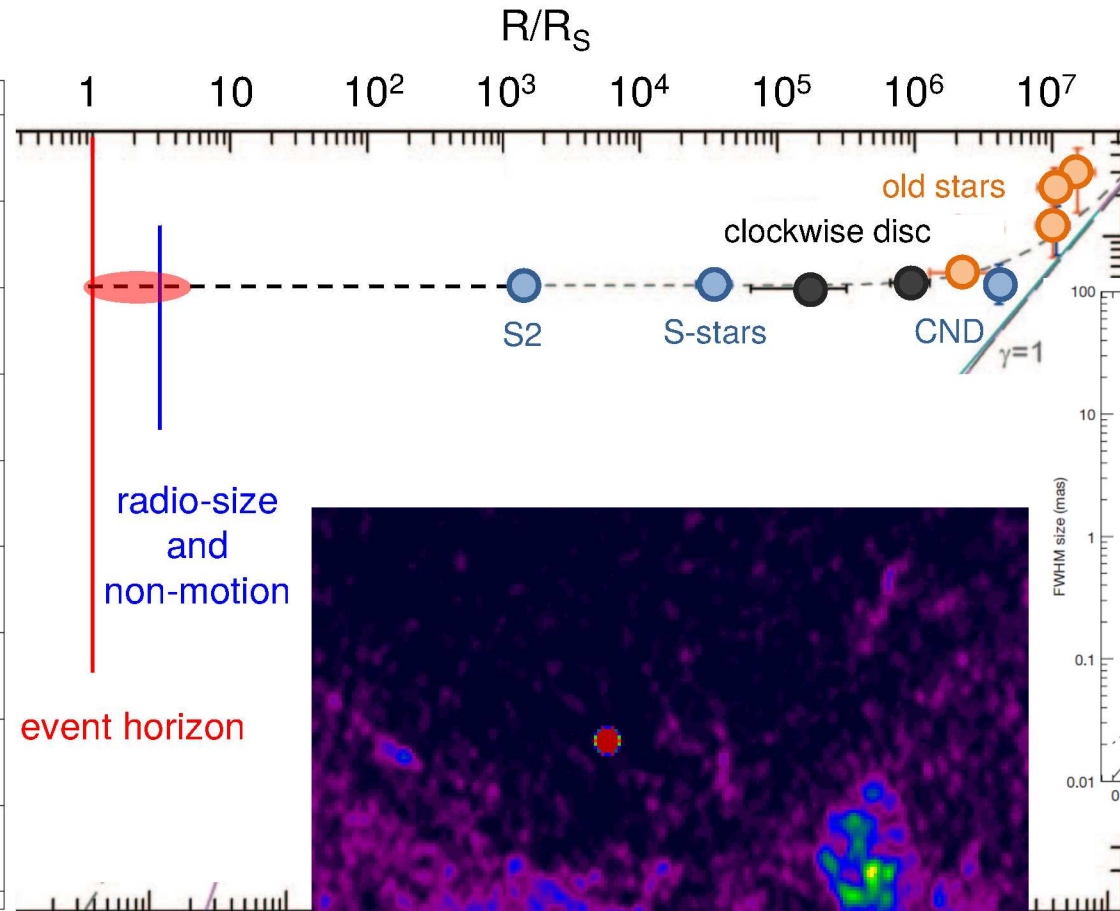


Culmination of 40 Years of Enclosed Mass Measurements

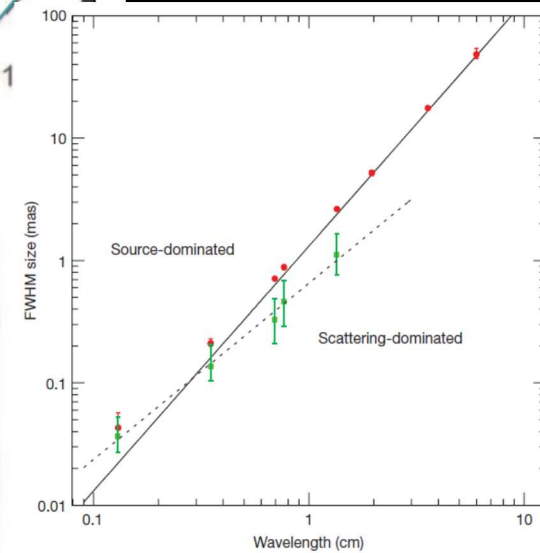
> 400000 M_{Sun}



Reid&Brunthaler04
Reid+08



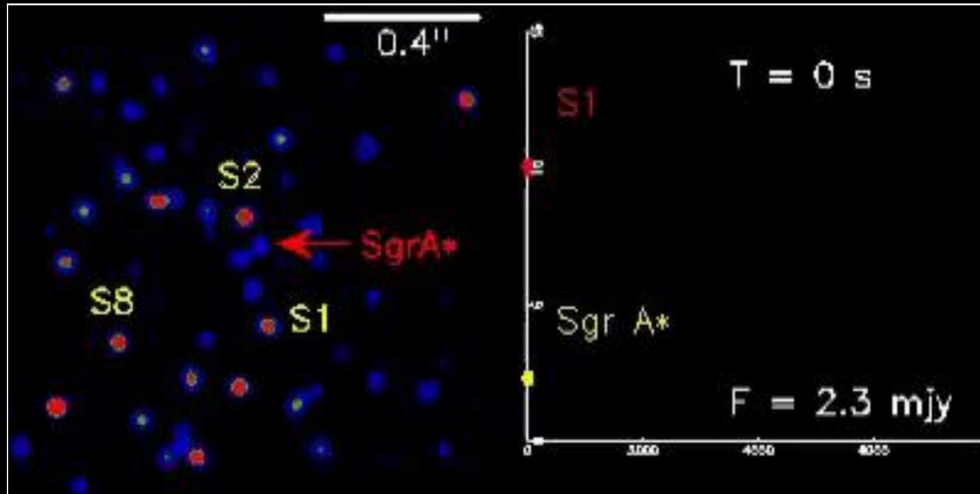
Smaller 3.7 R_S



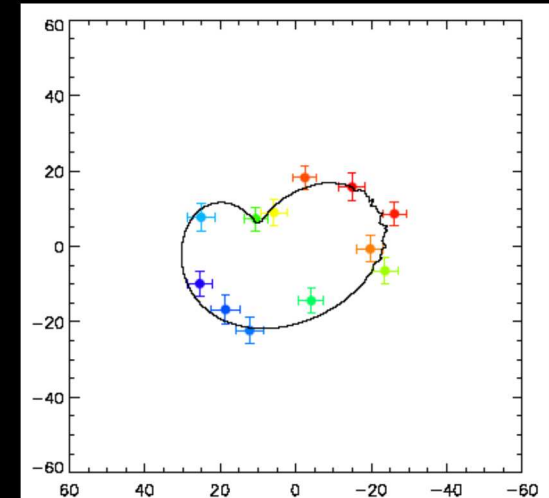
10

Krichbaum+98, Bower+04,06,
Shen+05, Fish+11, Doeleman+08

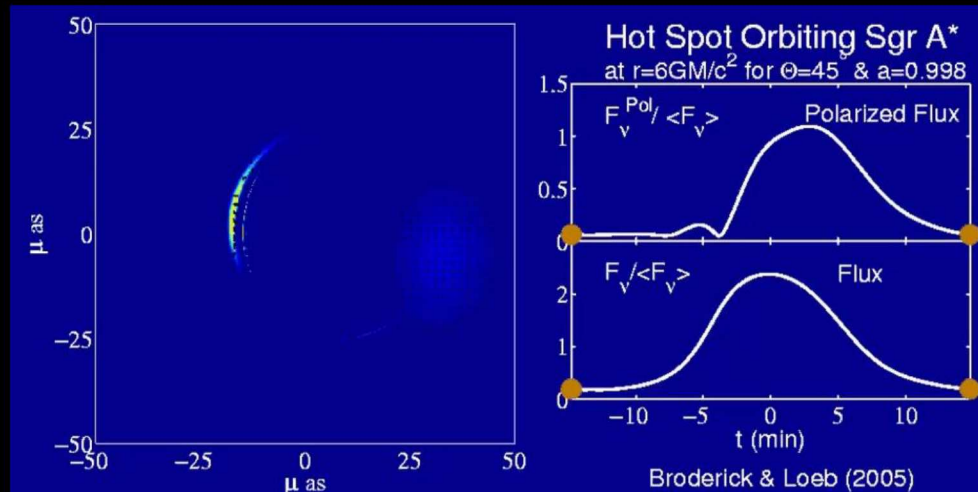
Hope for a Dynamical Mass Measurement at R_s Scale ?



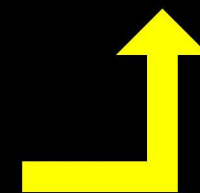
Genzel+03, Meyer+06/7, Trippe+07, Dodds-Eden+09,
Hamaus+09, Zamaninasab+10, Karssen+17



Eisenhauer+05

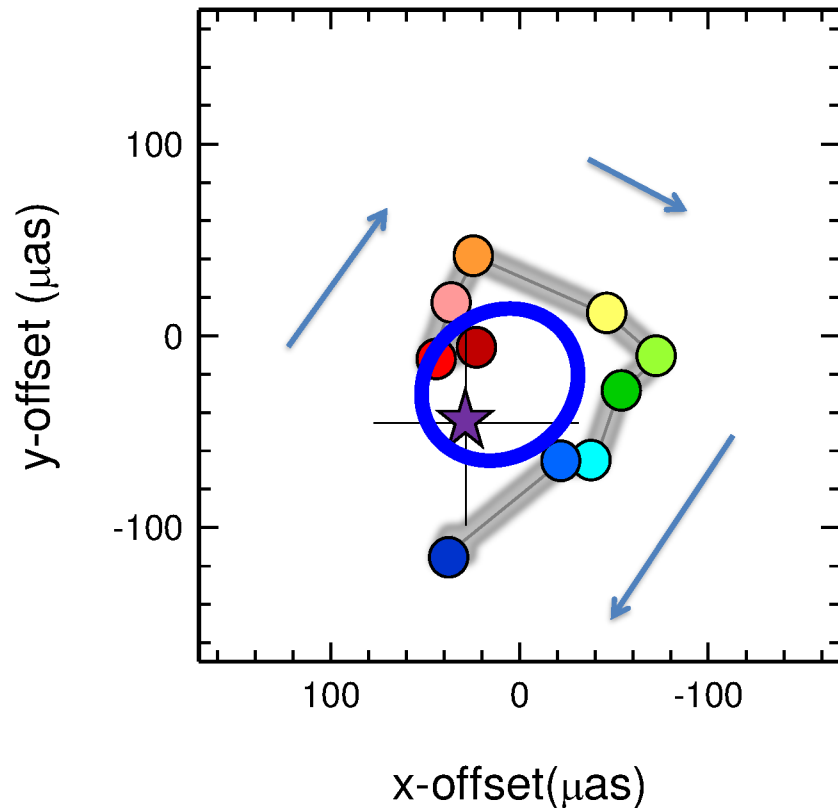


Broderick&Loeb05, Paumard05



GRAVITY Flare 22 July 2018

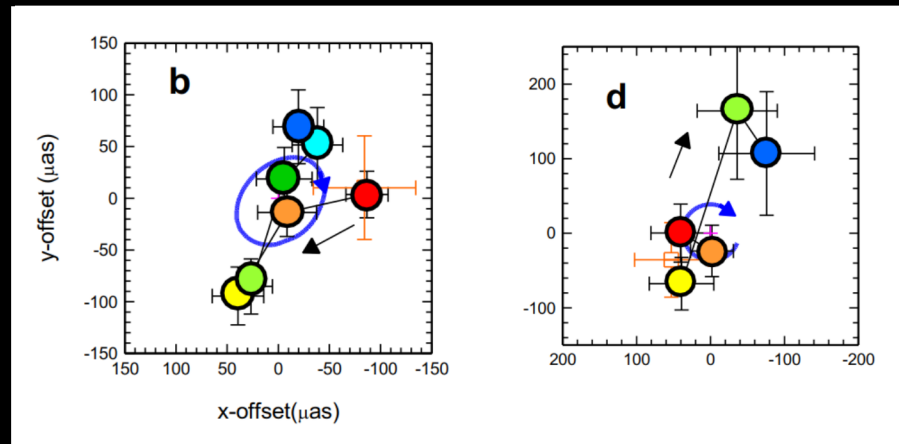
— $R=7 R$ $a=0$ $i=160^\circ$ $\Omega=160^\circ$ $\gamma^2=1.2$



- Clockwise, Looped Motion
- 150 μas Scale
- Few Ten Minutes

Circular Motion at about
30% Speed of Light

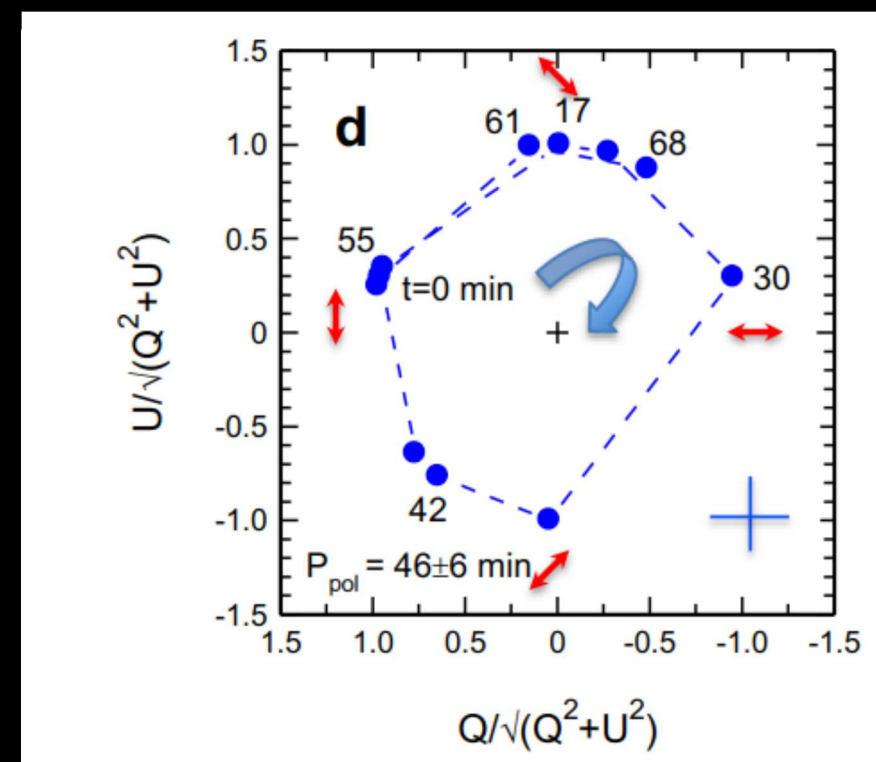
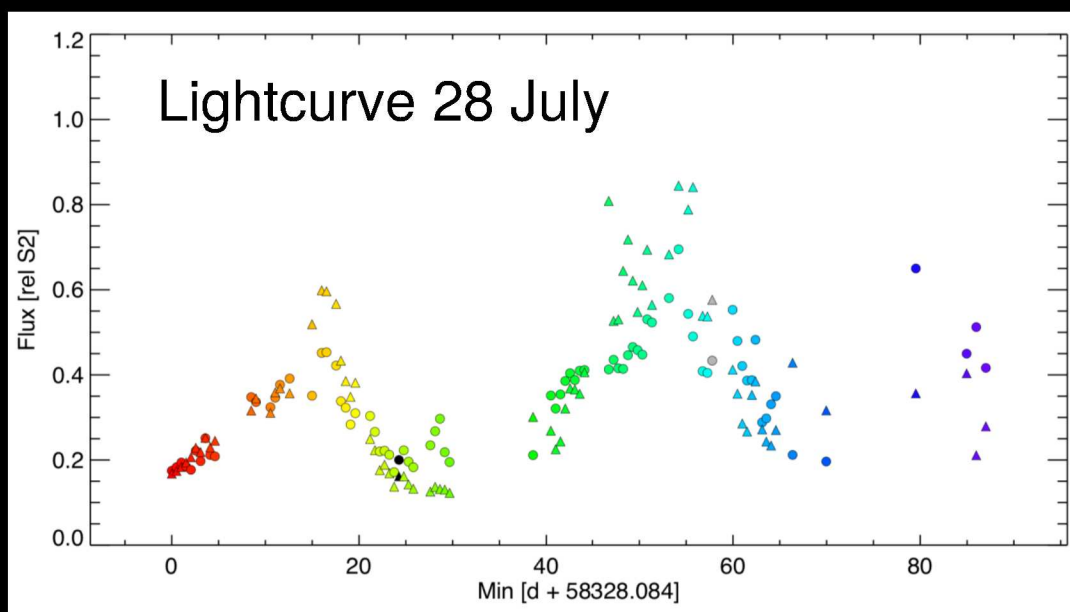
Again on 28 July and back on 27 May



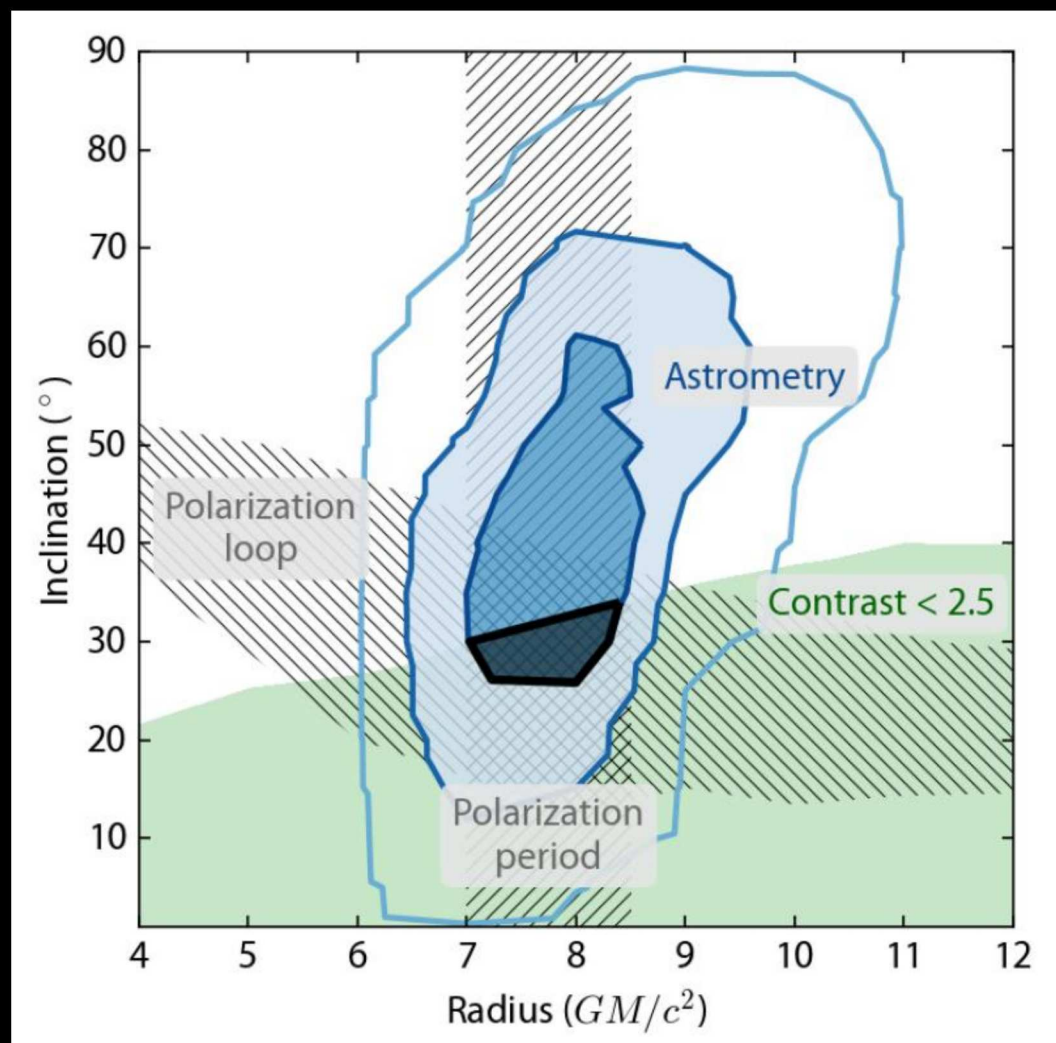
Low Inclination Circular Orbit Near Last Stable Orbit

Supported by **Low Relativistic Beaming Factor**

and **High Polarization Rotating with Orbit**

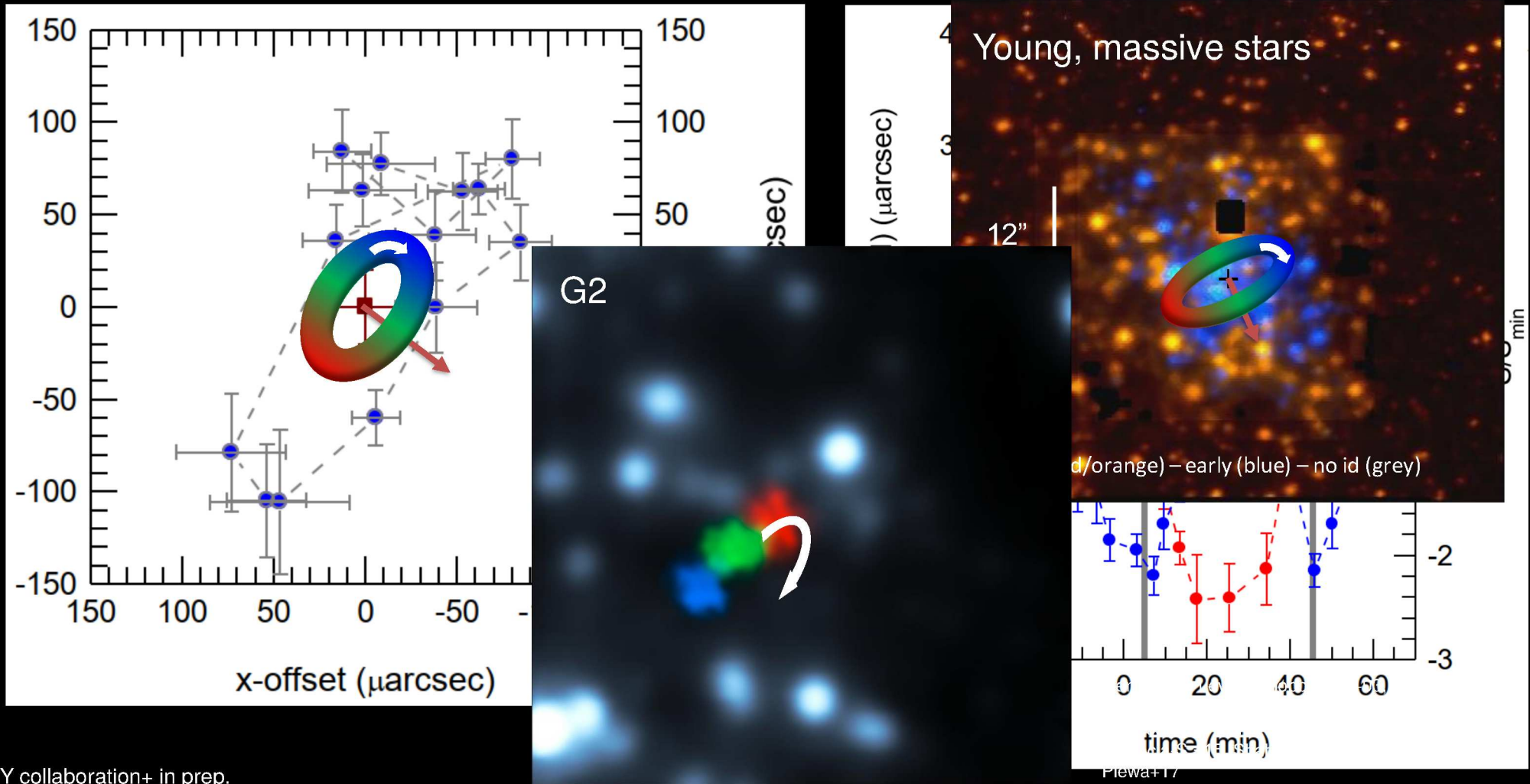


Low Inclination Circular Orbit Near Last Stable Orbit

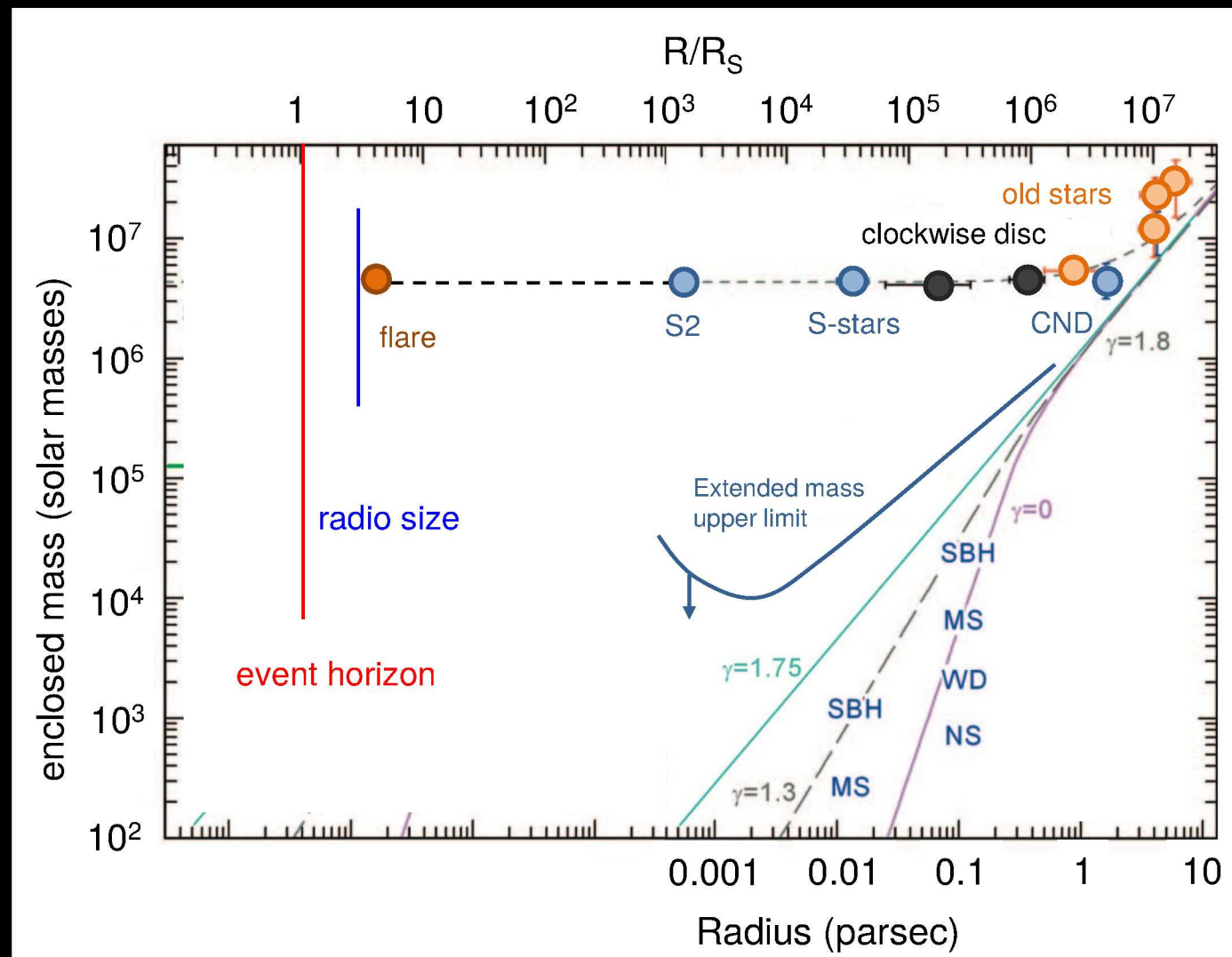


Again in April 2019 – Average of the Best Three Flares

Angular momentum orientation comparable to **stellar disc** and **infalling gas cloud**



Best Model Independent Case for Massive Black Holes



GRAVITY collaboration

Test of General Relativity **in the Galactic Center**

LIGO Gravitational Waves

Fe K α line

Shadow of M87 Black Hole

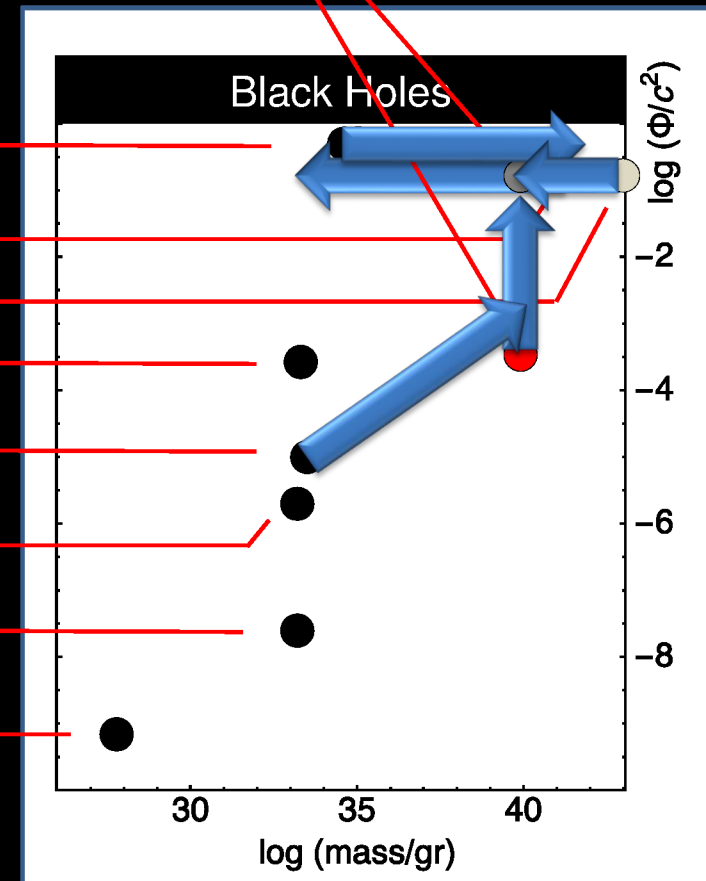
Sirius B

Hulse-Taylor Pulsar

Light Deflection & Shapiro Delay

Precession of Mercury

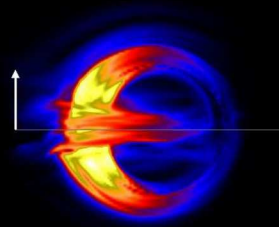
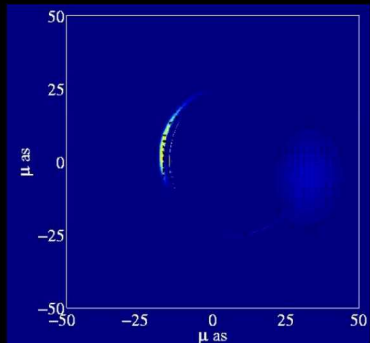
Pound-Rebka



Adapted from Psaltis04

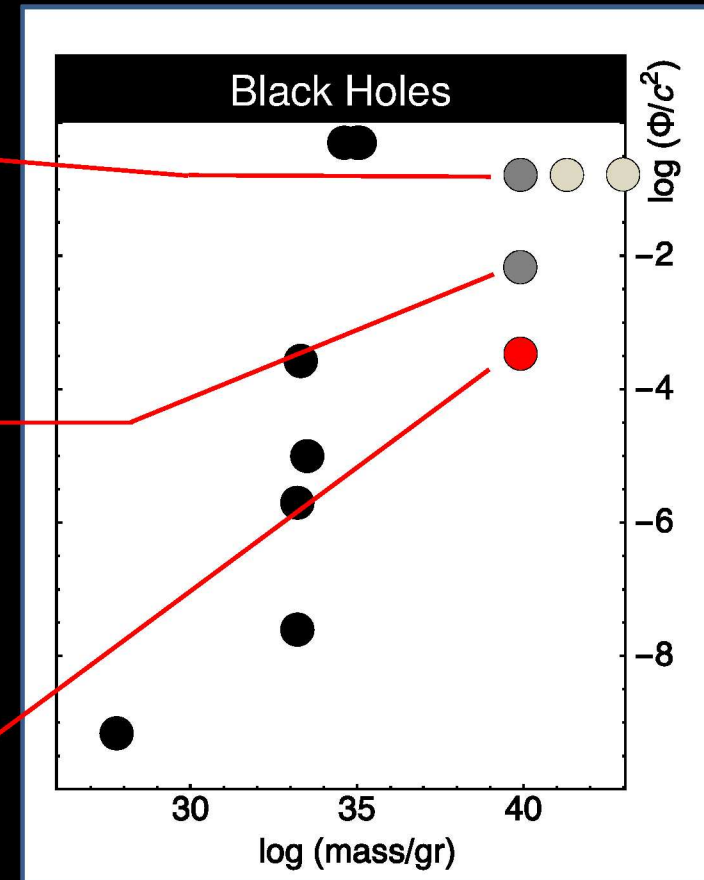
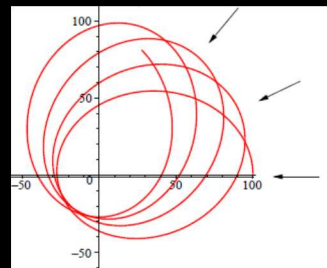
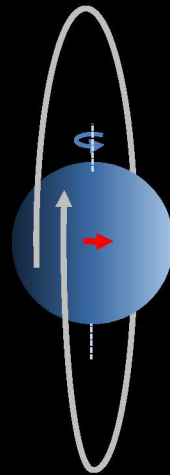
Test of General Relativity in the Galactic Center

Flares & Shadow from Sgr A*

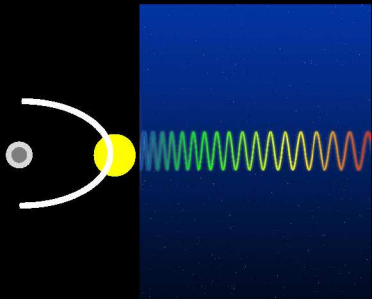


Lense Thirring
Precession

Periastron Shift



Gravitational Redshift



Flares: GRAVITY collaboration+18, Broderick,Loeb+05, Paumard+05, Hamaus+06,Vincent+16,
Shadow: McKinney, Blandford+, Falcke, Dexter, Agol+, Mościbrodzka, Gammie, Dolence+, Broderick, Loeb+, Shcherbakov, Penna+
Lense Thirring: Kraniotis07, Will08, Kannan&Saha09, Merritt+10, Angéllil+10,11, Iorio11, Zhang+15,17, Yu+16, Grould+17, Waiserg+18
 β^2 effects: Jaroszynski 98, Rubilar&Eckart 01, Fragile&Mathews 00, Alexander 05, Weinberg+05, Zucker+06, Angelil+10, Hees+17, Parsa+17, Grould+17, Nishiyama+18

Probing PPN with Stellar Redshifts

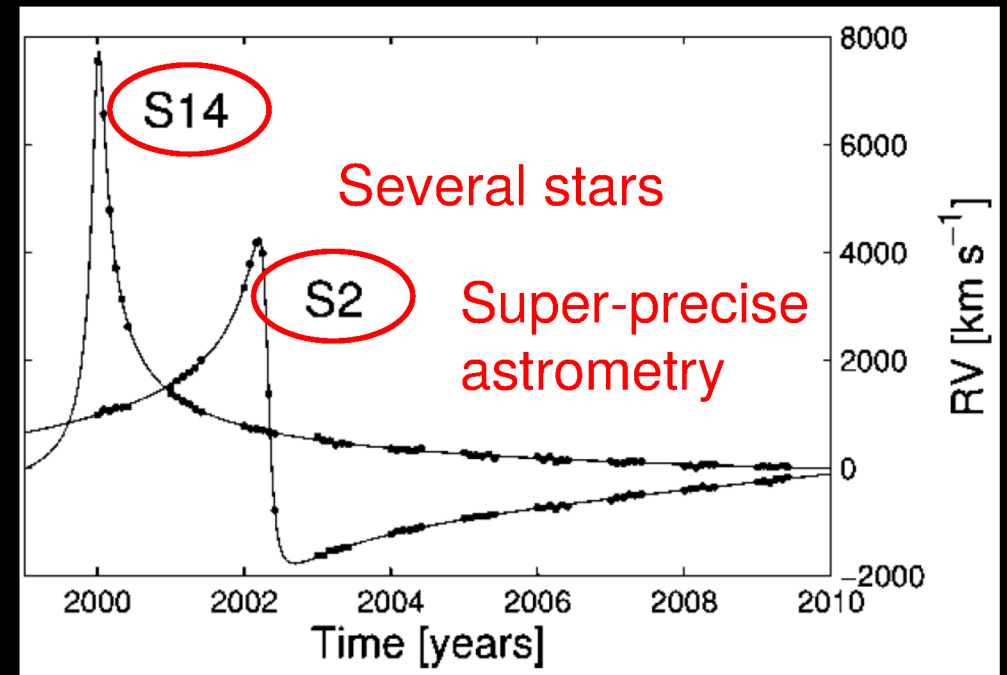
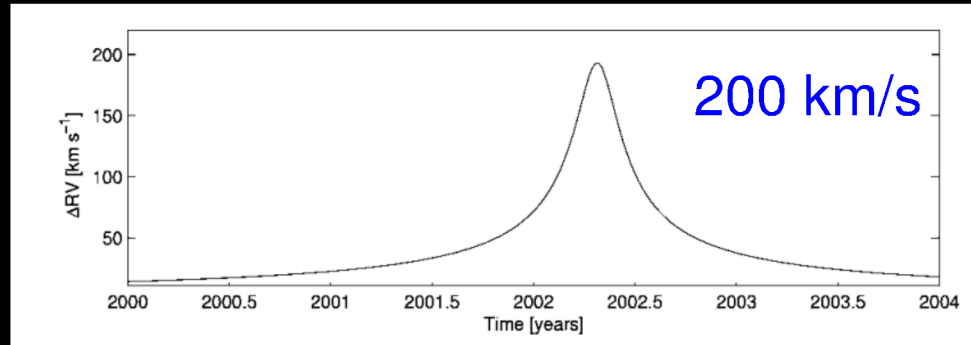
Redshift

$$z = \Delta\lambda/\lambda = B_0 + B_1\beta + B_2\beta^2$$

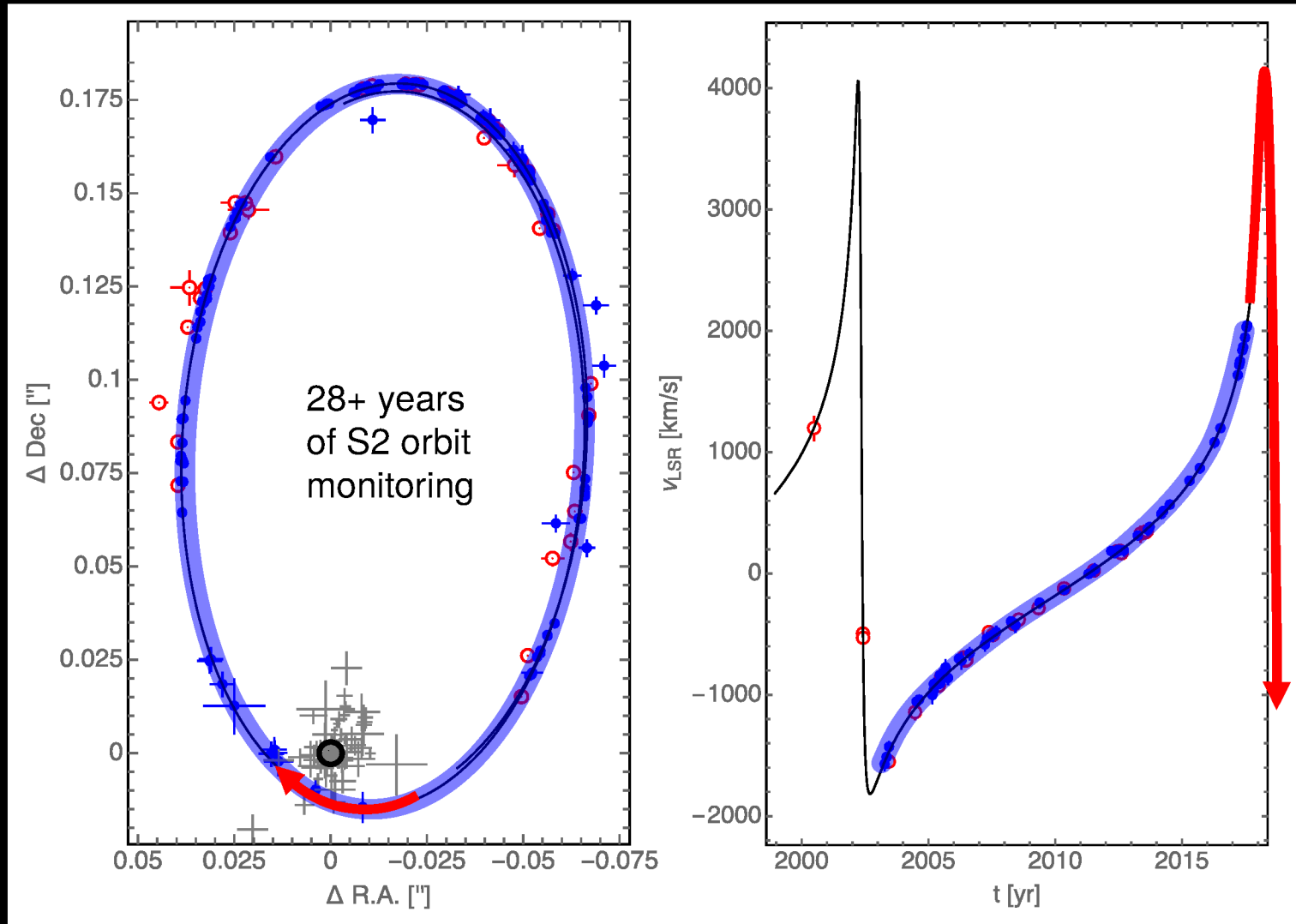
$$\text{PPN}(1) \sim \Upsilon(r_p) \equiv r_s/r_p \sim \beta^2$$

$$\sim 6.5 \times 10^{-4}$$

But radial velocity alone
not enough, because
relativistic effect can be
absorbed in Kepler
orbital elements

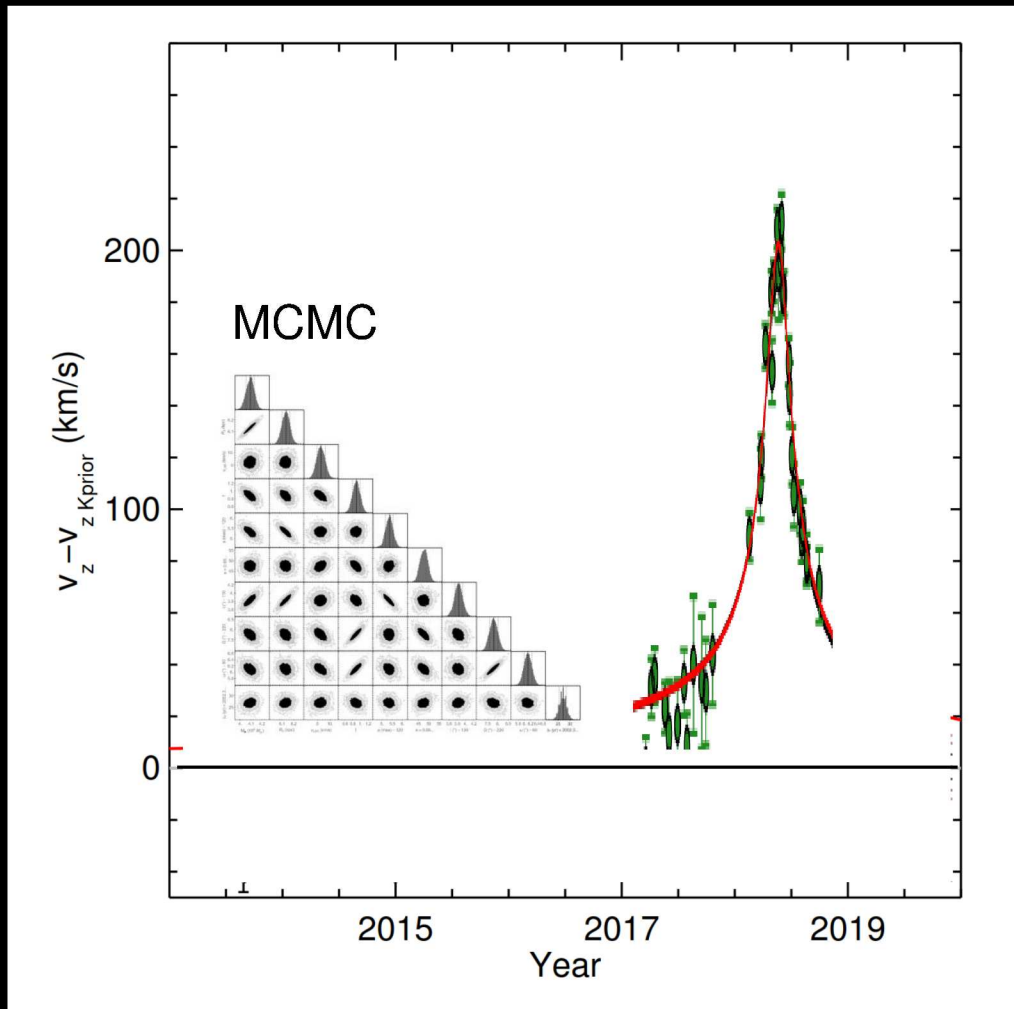


Measuring the Gravitational Redshift at Closest Approach



Schödel+02, Eisenhauer+03,05, Ghez+05,08, Gillessen+09,17, Mayer+12, Boehle+16, Sakha+19, GRAVITY collaboration+18,19

A Posteriori Analysis



$f = 0$: Newton
 $f = 1$: General
Relativity

→ Excludes prior
Newtonian orbit at 20σ

Such high significance
only possible with
precise knowledge of
orbital parameters

Uncertainty of the radial
velocity prediction from
Kepler fit to data up to 2017

Gravitational Redshift is **More Fundamental** than GR

$f = 0$: Newton

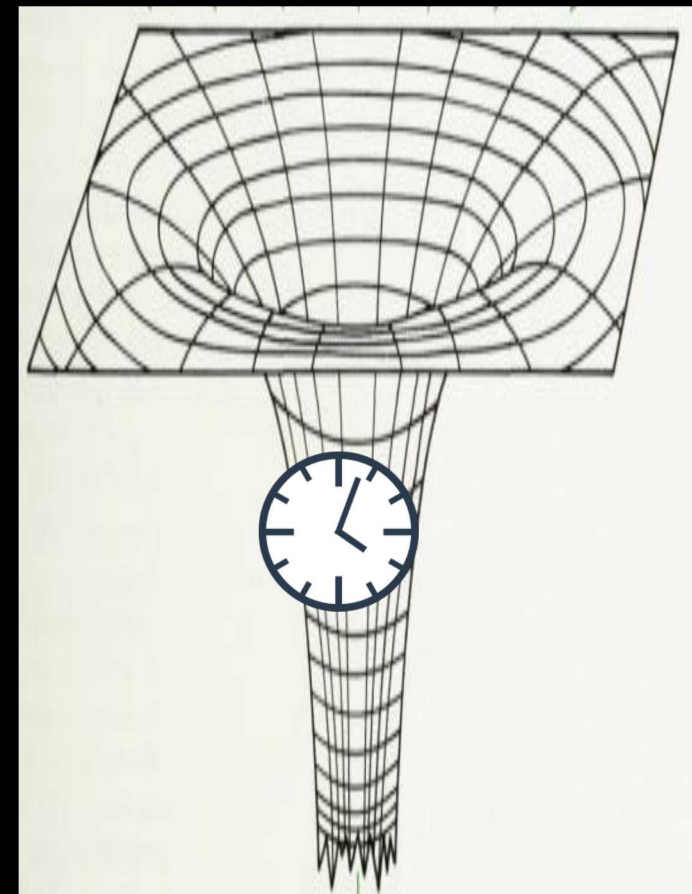
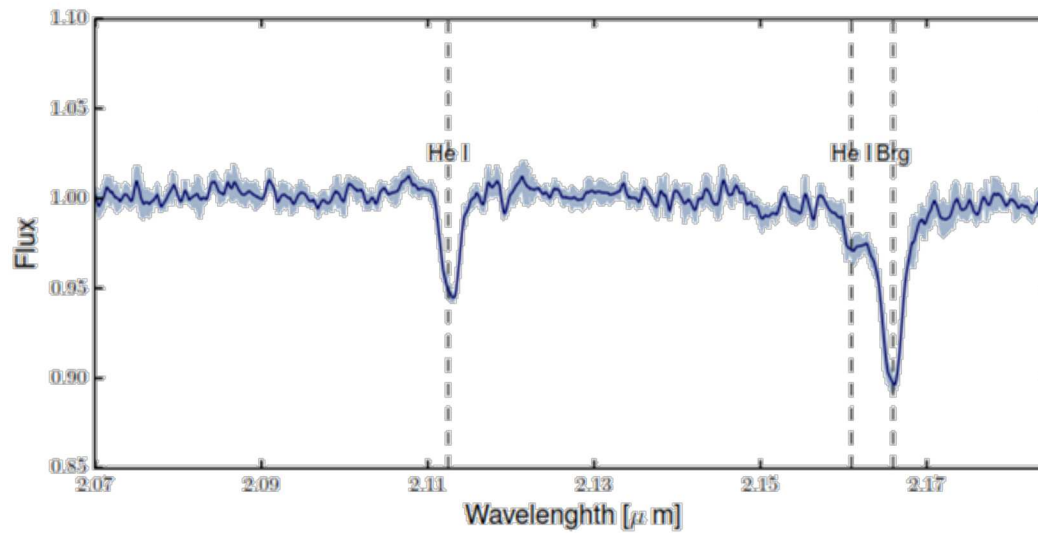
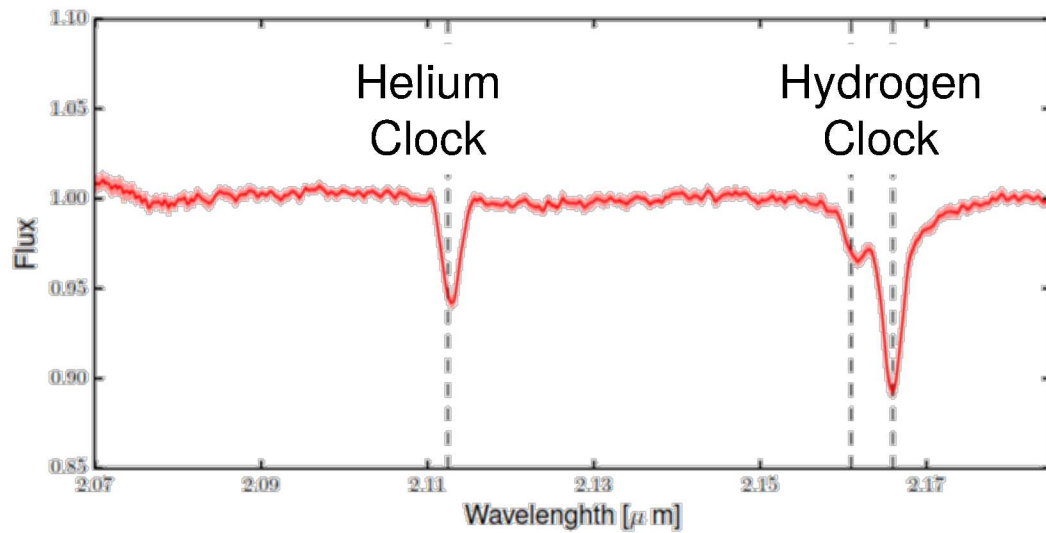
$f = 1$: General
Relativity

→ $f = 1.04 \pm 0.05$

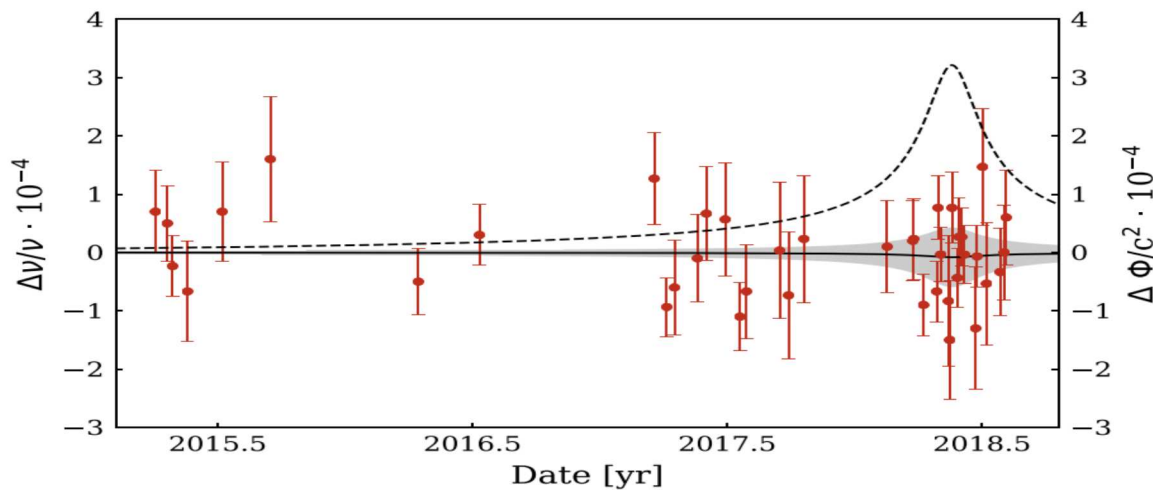
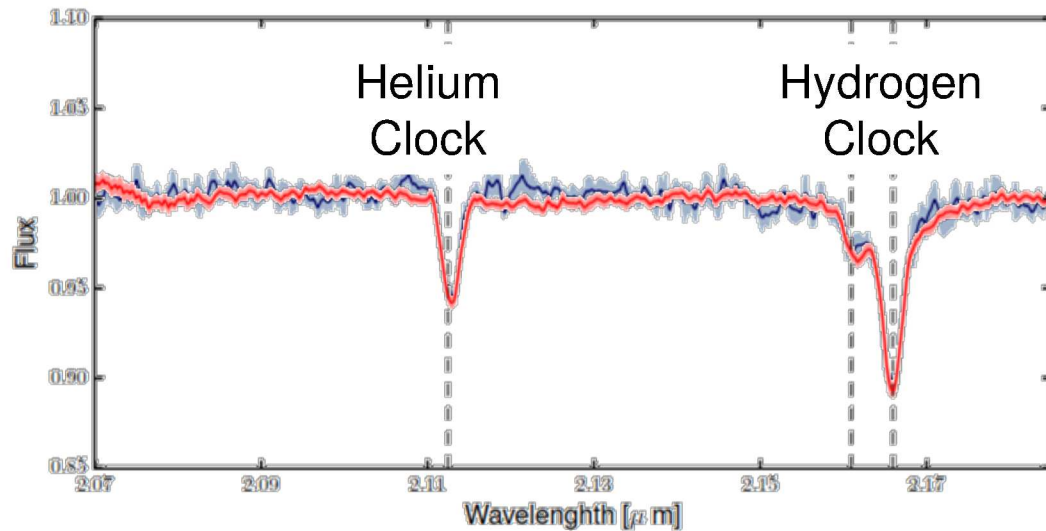
Does **not** distinguish
between GR and any other
metric theory of gravity, but
is only a test of the **Einstein
Equivalence Principle**

Will 06, Angelil&Saha10

Testing the Local Position Invariance (LPI)



Local Position Invariance for Different Clocks



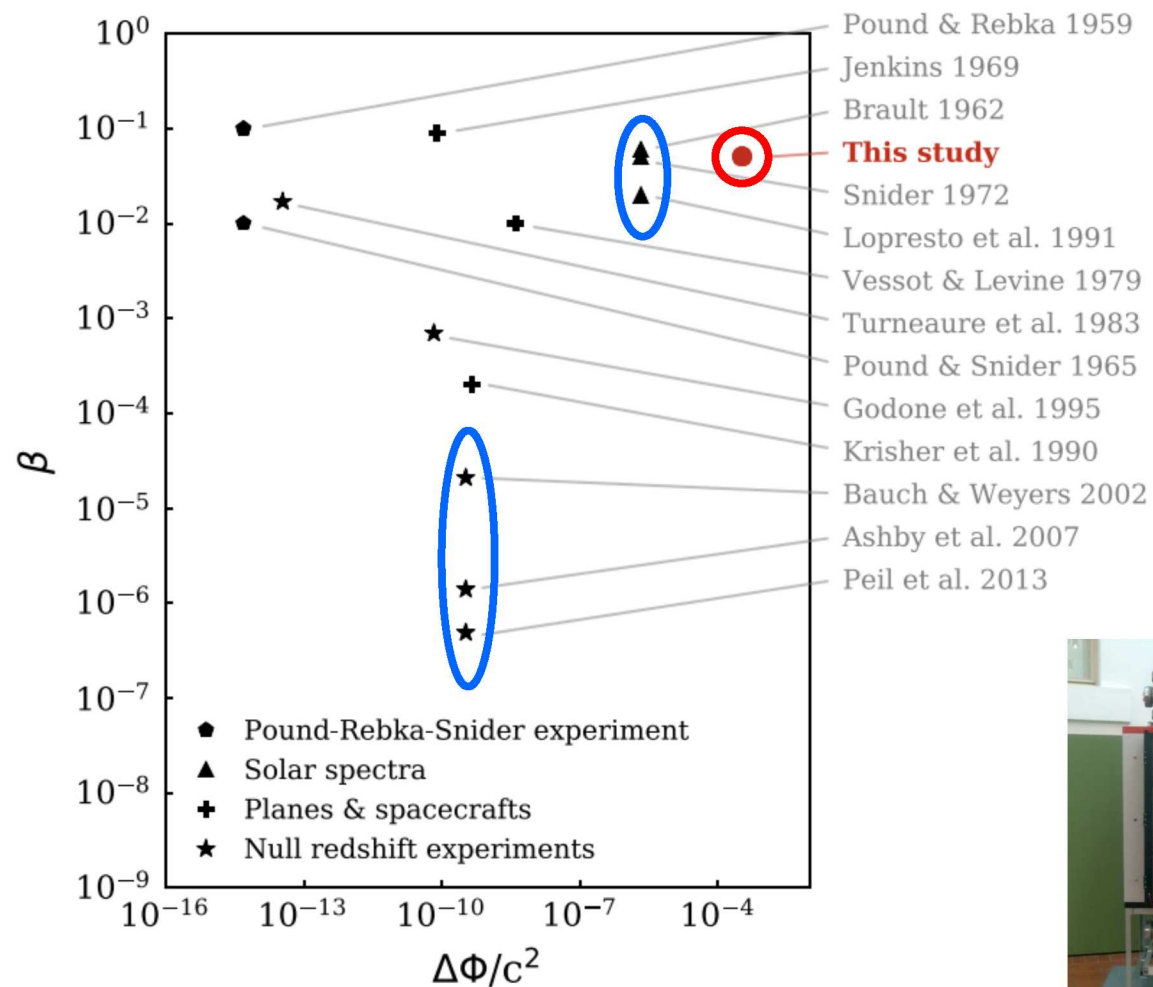
$$\frac{\Delta f}{f} = \Delta z_{\text{Clock1} - \text{Clock2}} = \frac{\Delta\alpha}{\alpha} \left(\frac{\Delta\Phi}{c^2} \right)$$

Galactic Center

$$\left(\frac{\Delta\alpha}{\alpha} \right)_{\text{HeI} - \text{Br}\gamma} = 2.4 \pm 5.1 \%$$

for $\left(\frac{\Delta\Phi}{c^2} \right) = 3 \times 10^{-4}$

LPI Tested in Orders of Magnitude Stronger Potentials

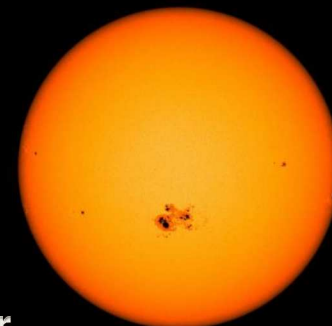


Sun / Infrared Oxygen Triplet

(e.g. Brault63, Snider72, Lopresto+91)

$$\left(\frac{\Delta\alpha}{\alpha}\right)_{O \lambda 7772-7775} < 10^{-2}$$

for $\left(\frac{\Delta\Phi}{c^2}\right) = 4 \times 10^{-6}$



Galactic Center

$$\left(\frac{\Delta\alpha}{\alpha}\right)_{HeI - Br\gamma} = 2.4 \pm 5.1 \%$$

for $\left(\frac{\Delta\Phi}{c^2}\right) = 3 \times 10^{-4}$

Atomic Clock vs. H-Masers

(Bauch&Weyers02, Ashby+07, Peil+13)

$$\left(\frac{\Delta\alpha}{\alpha}\right)_{Rb-H} < 10^{-6}$$

for $\left(\frac{\Delta\Phi}{c^2}\right) = 3 \times 10^{-10}$

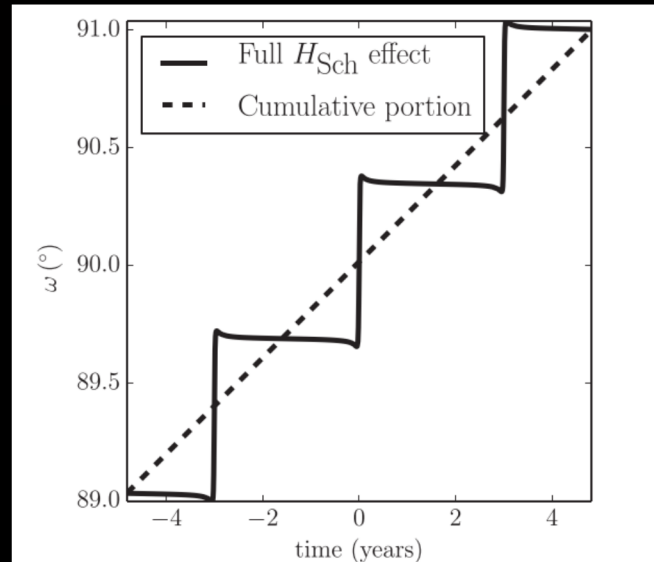


The Next Step – Schwarzschild Precession

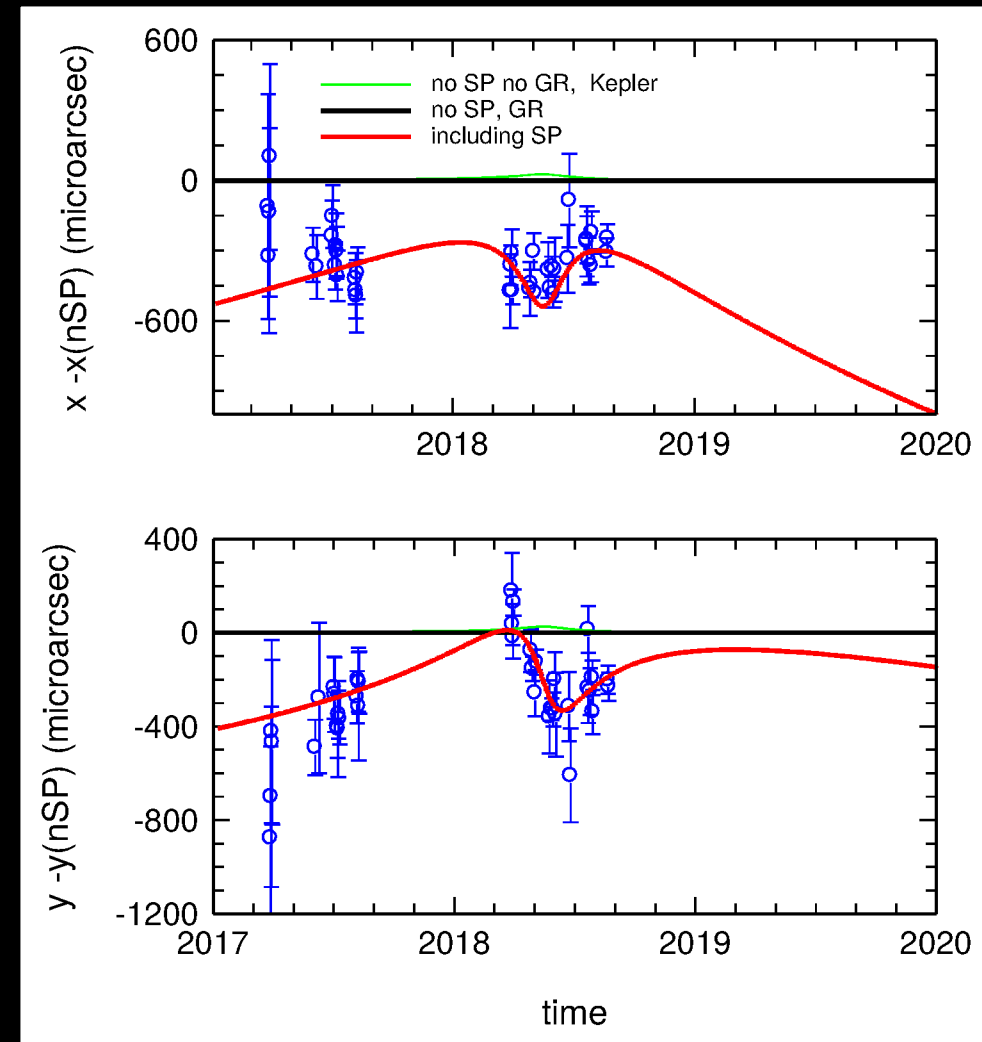
$$\Delta\varphi = \frac{6\pi G}{c^2} \frac{M}{a(1-e^2)} \sim 11.9' \sim 800 \mu\text{as}$$

Mar – Aug $\Delta\text{RA} \sim 50 \text{ mas}$
 $\rightarrow \Delta\varphi = 200 \mu\text{as}$

Currently about **2 σ**



Angelil&Saha14



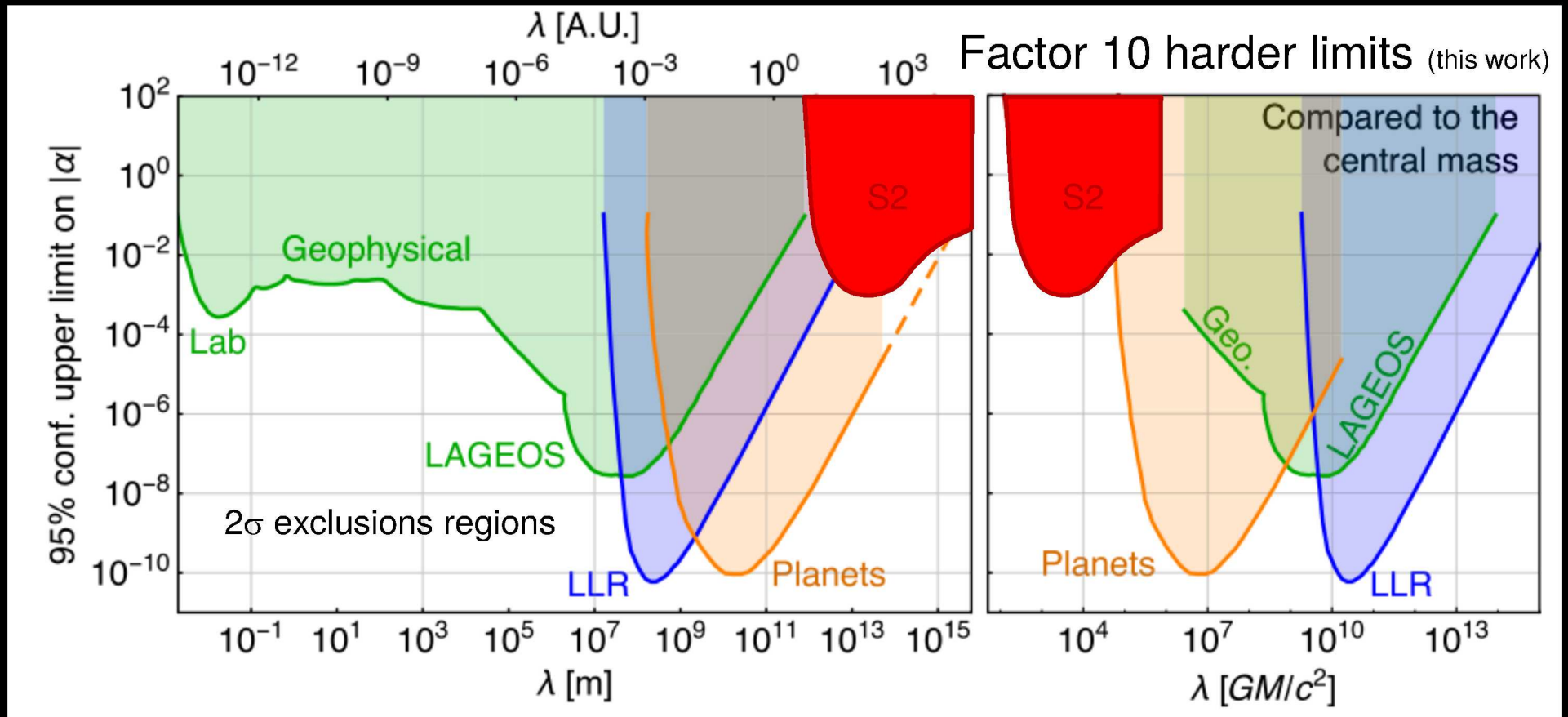
GRAVITY collaboration



Jaroszynski98
 Fragile&Mathews00
 Rubilar&Eckart01

New Physics – Fifth Force ?

Phenomenological via Additional Yukawa Potential $U = \frac{G M}{r} \left(1 + \alpha e^{-r/\lambda} \right)$



Scalar Tensor Gravity

Gravina+18
Jovanovic+19

Tidal Charge

Horvat&Gergely13

Hees+17 GRAVITY collaboration+19, in prep.

Grand Quests for the Future

Spin of the Black Hole

$$V_{\text{eff}}(r, e, l) = -\frac{M}{r} + \frac{l^2 - a^2(e^2 - 1)}{2r^2} - \frac{M(l - ae)^2}{r^3}$$

$$a \equiv \frac{J}{M}$$

Cosmic Censorship

$$a > 1$$

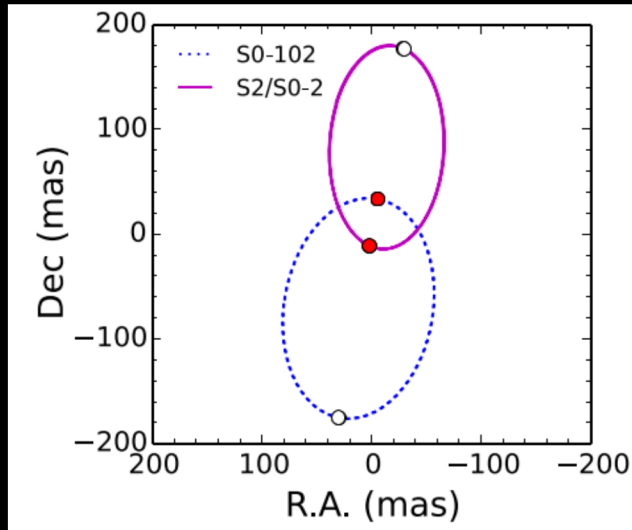
Naked Singularity

No Hair Theorem

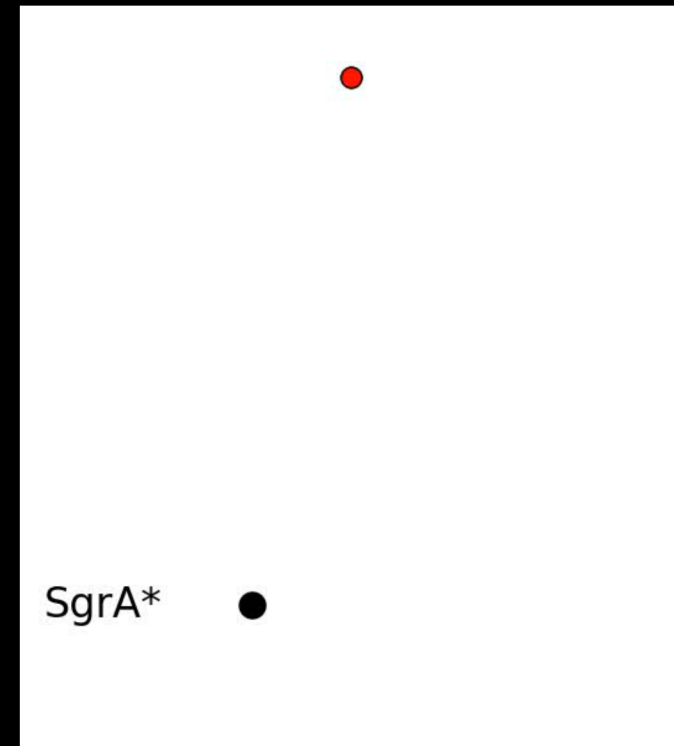
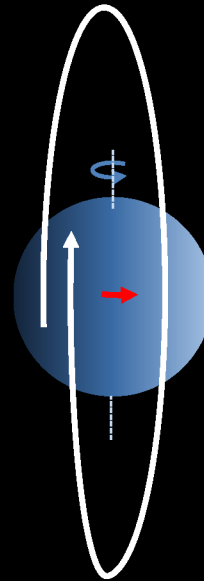
$$Q_2 = -J^2/M$$

Quadrupole Moment

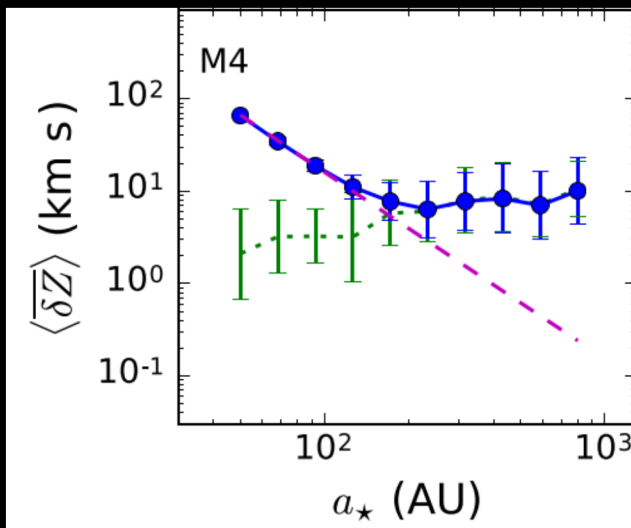
Model Independent Spin Measurement



Already **known stars obscure spin** in S2 orbit

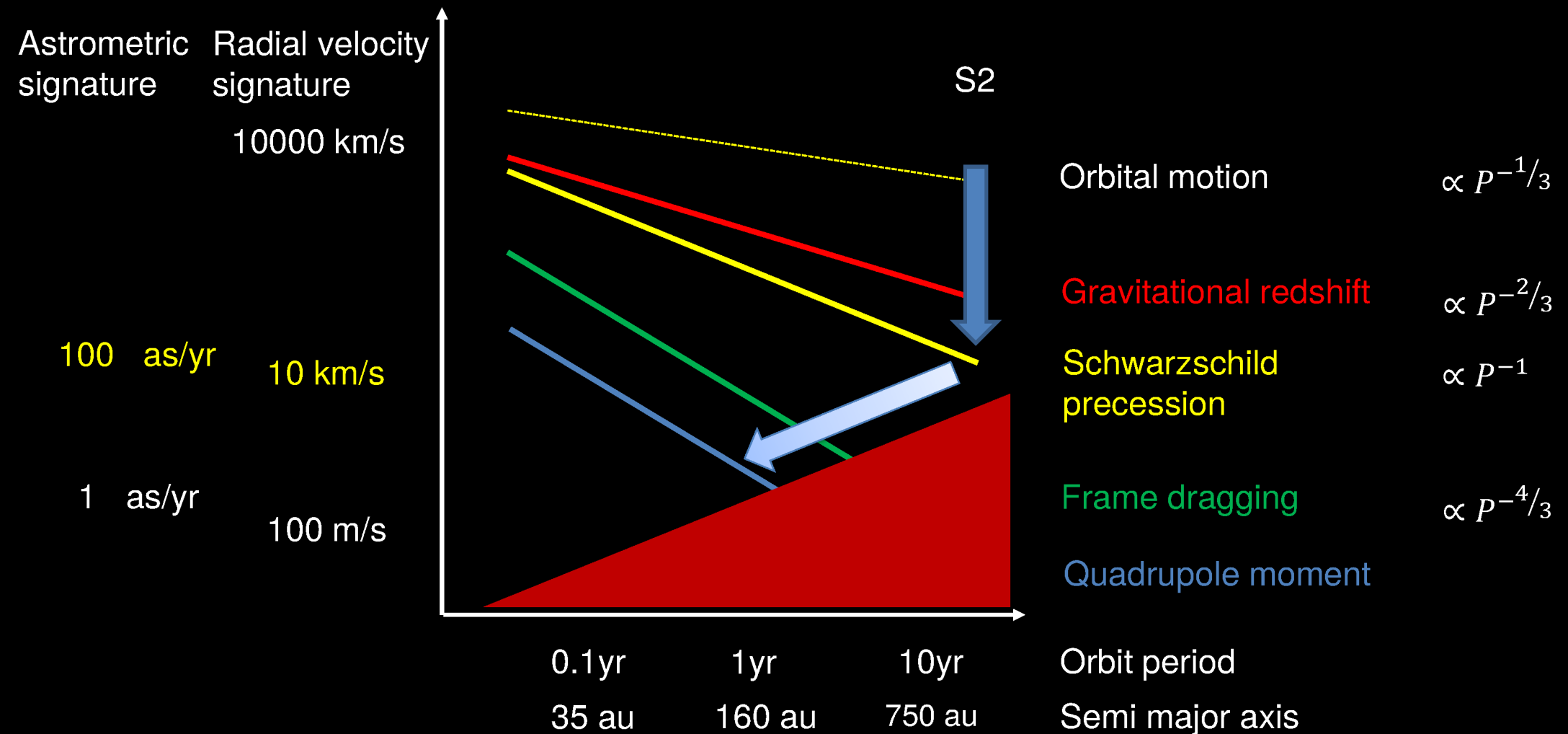


Newtonian Perturbations
To be on safe side **“S2/10”**



We should have about $\lesssim 1$ star
with $K \sim 20$ fulfilling criteria

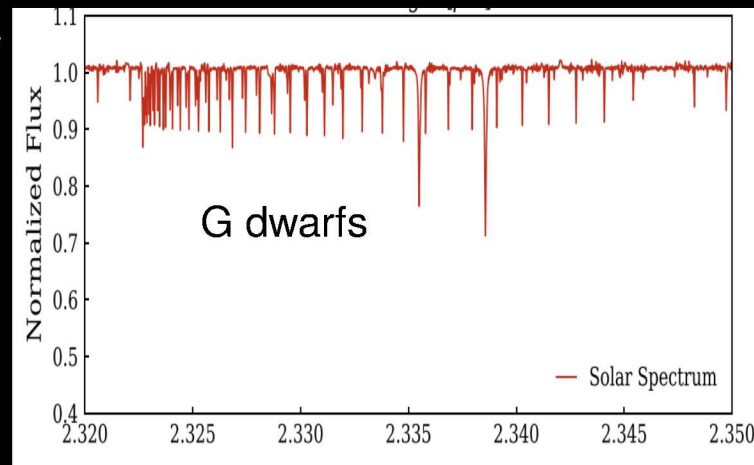
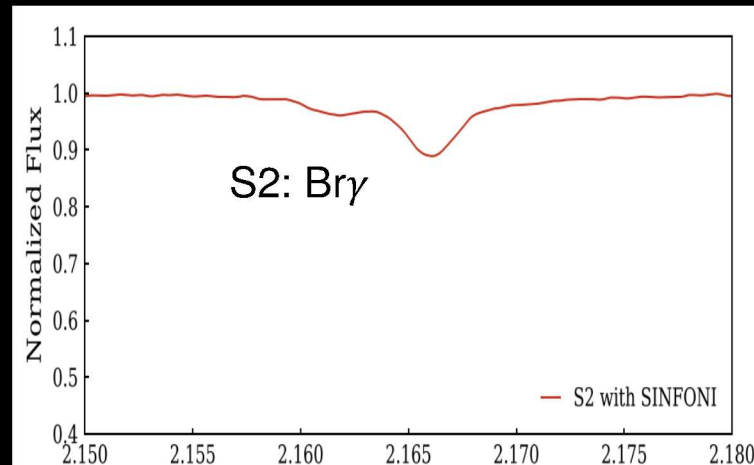
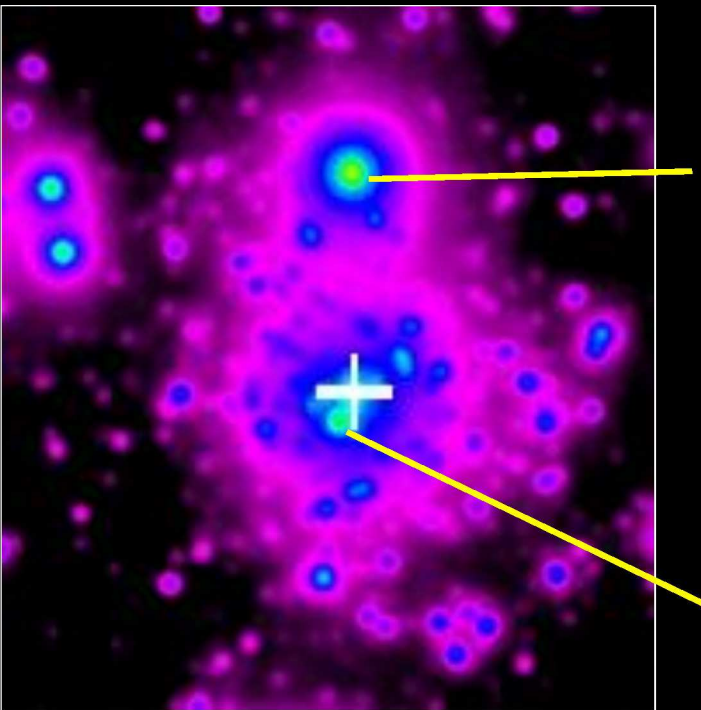
Towards a Spin Measurement – How To Get There



Towards a Spin Measurement – How To Get There

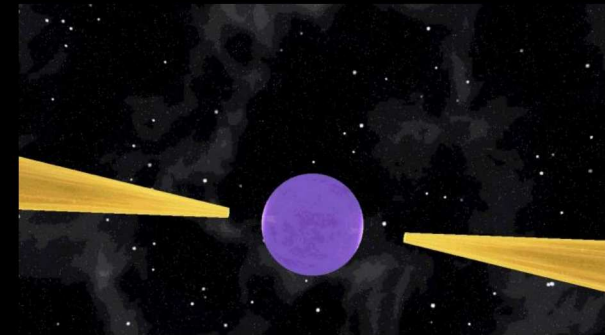
Spectroscopy

Extremely Large Telescope



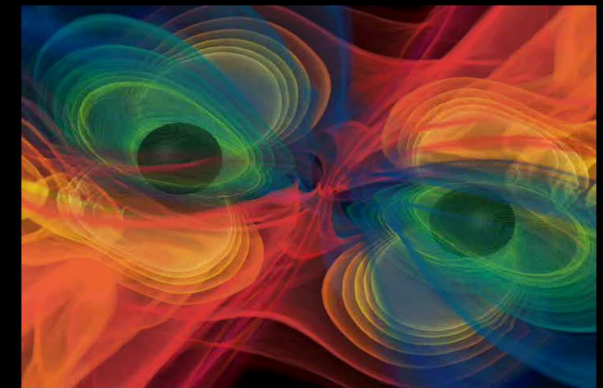
And Bring Together Hard, Independent Numbers

Pulsars



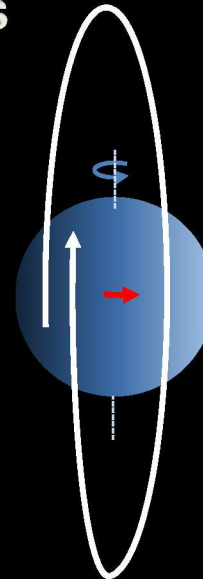
Wex&Kopeikin99, Liu12, Liu+14,
Psaltis,Wex,Kramer16, Eatough+13

Gravitational Waves



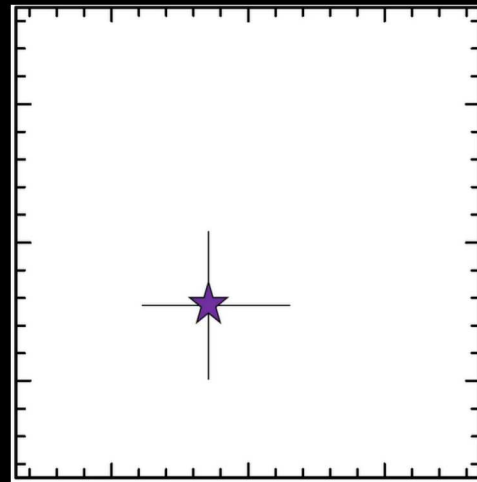
For SgrA* e.g. Gourgoulhon+19

Stellar orbits



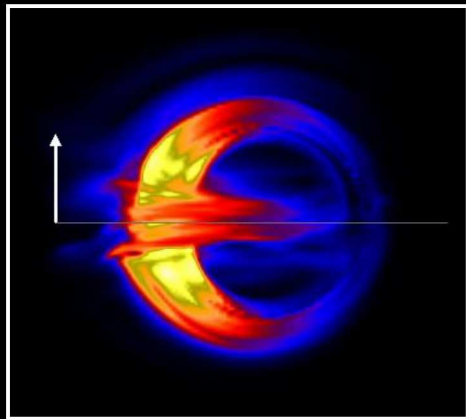
Kraniotis07, Will08,
Kannan&Saha09, Merritt+10,
Angéil+10,11, Iorio11,
Zhang+15,17, Yu+16,
Gould+17, Waiserberg+18

Flares



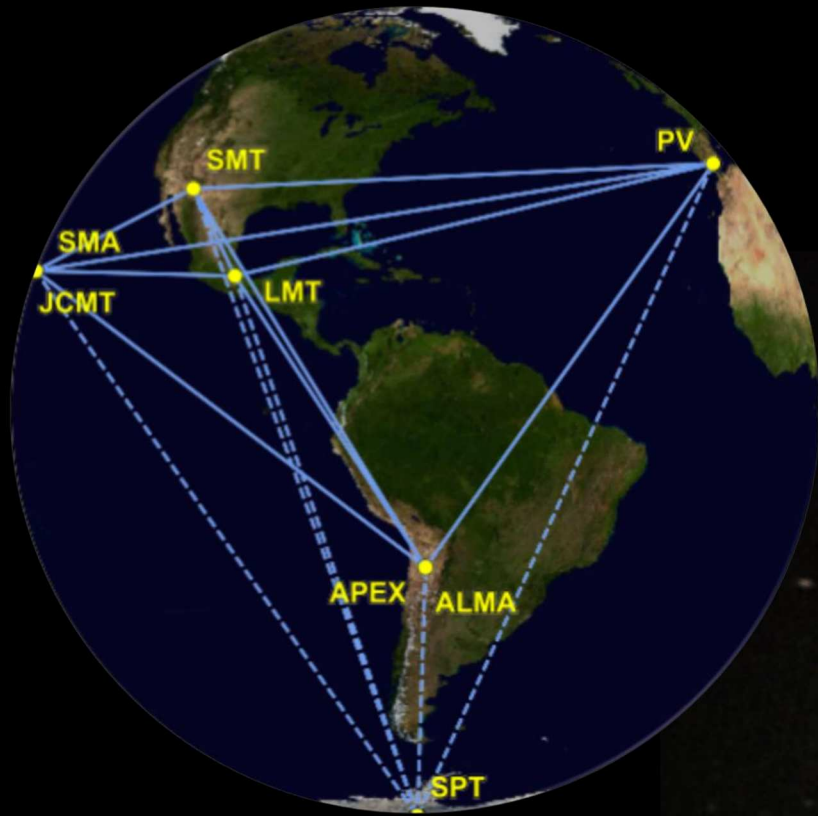
Baganoff+01, Ponti+18, Boyce+19
Genzel+03, Broderick&Loeb05,
Paumard+05, Hamaus+08, Vincent+16
GRAVITY collaboration+18

Shadow



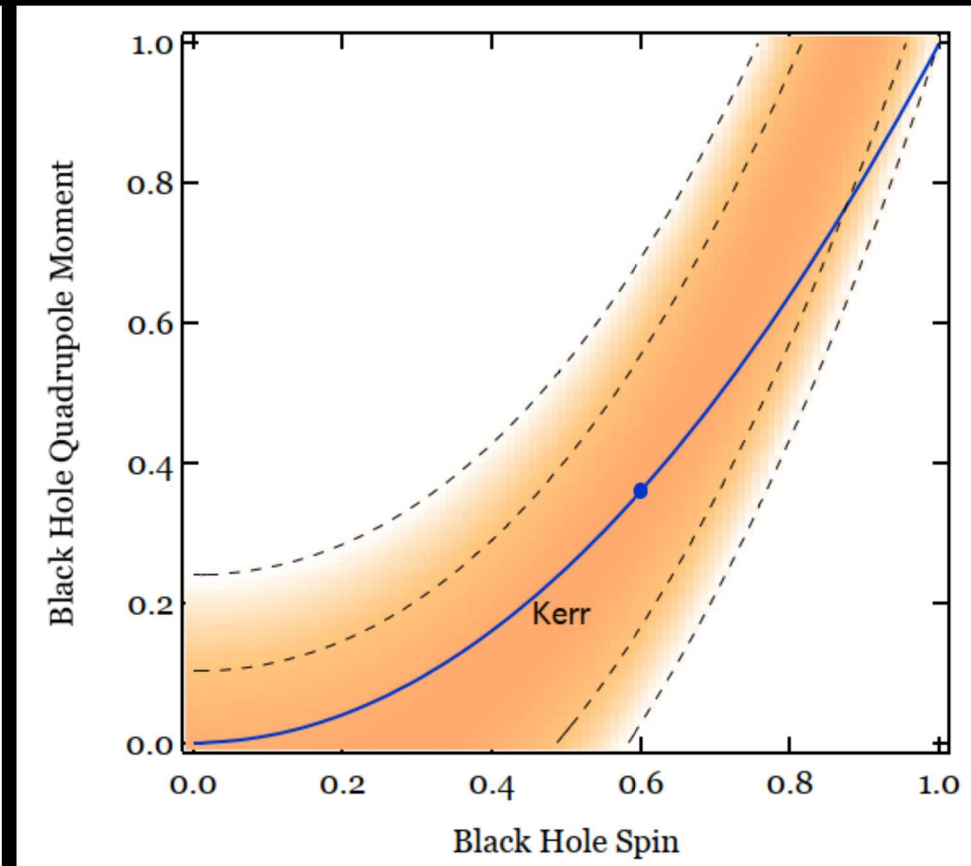
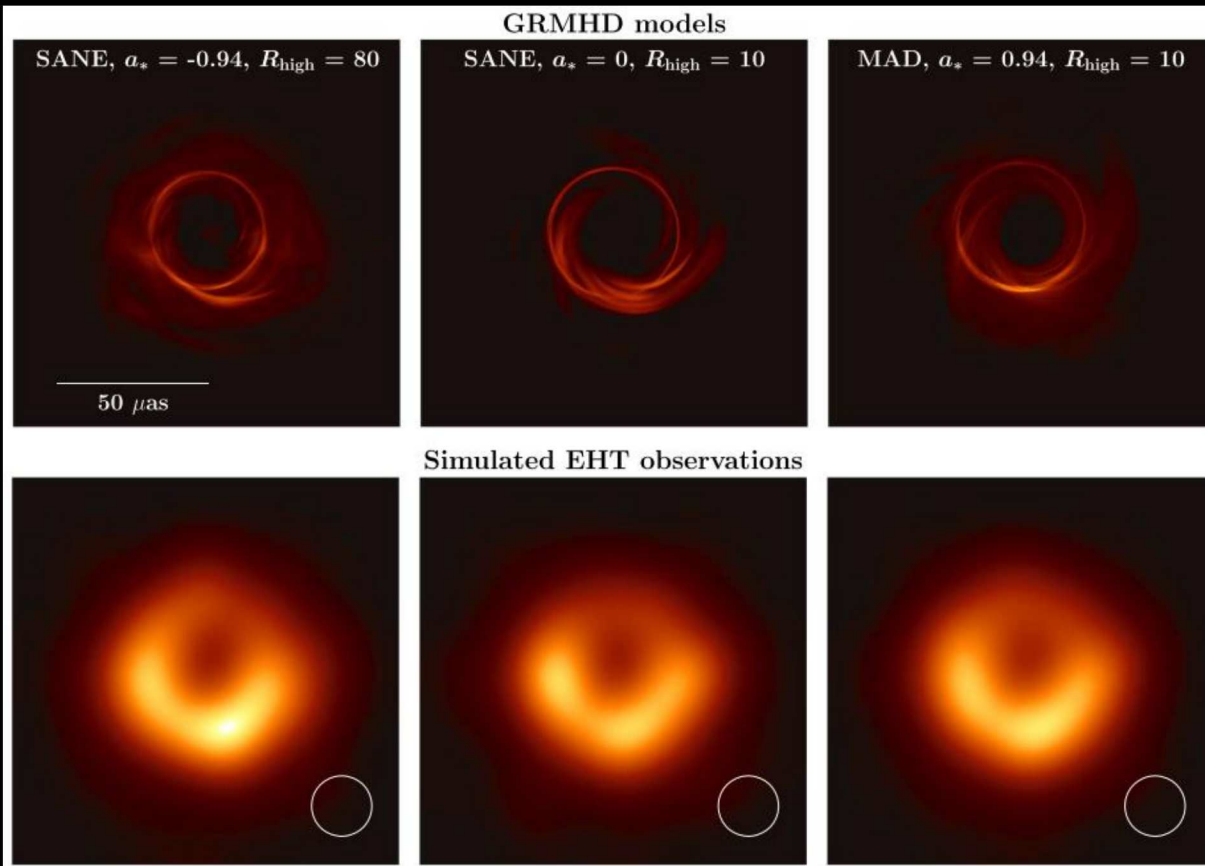
EHT collaboration
Dexter, Agol et al.,
Mościbrodzka, Gammie, Dolence et al.,
Broderick, Loeb et al.,
Shcherbakov, Penna, McKinney

Shadow Experiment – Following the Example of M87



Shape of Shadow – Tracer of Spin / Quadrupole Moment

Ringlike Structure $\sim 5 R_G$ very much **Modell Independent**

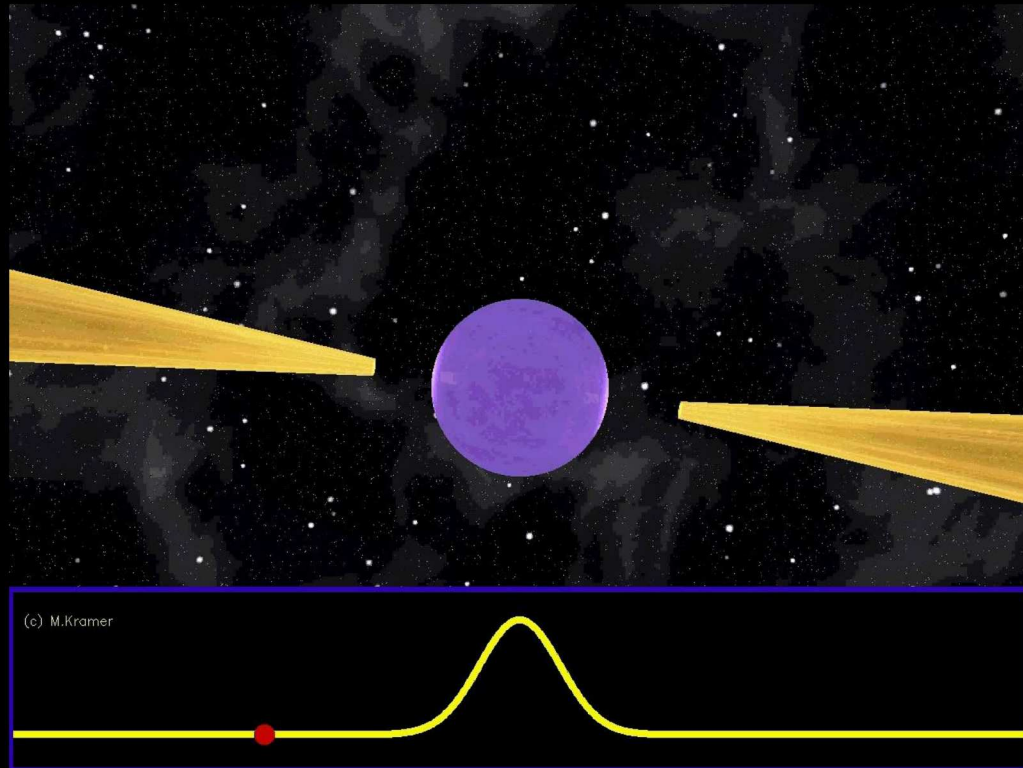


Pulsars – Perfect Timing

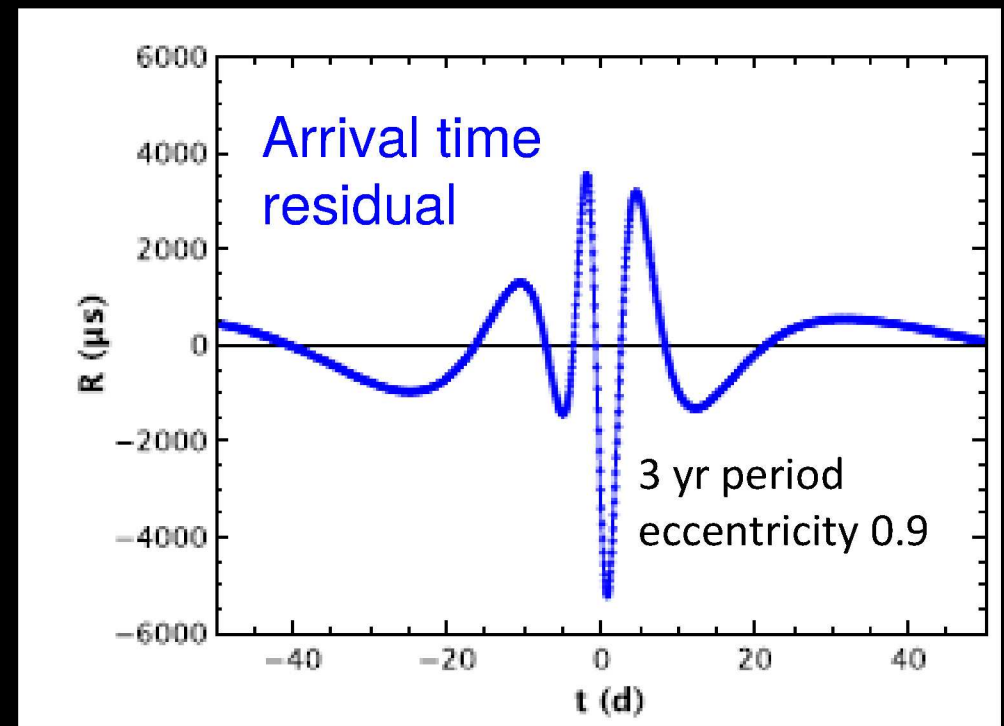
Hulse&Taylor76, Kramer+06, Weisberg+10

Exquisite Precision, e.g.
Periastron Advance for Binary
Pulsar PSR B1913+16:

4.226598(5) deg/yr



Clean signature of **Frame Dragging**
in Simulated Galactic Center Pulsar



Shadow Imaging and Pulsar Search are Difficult in the GC

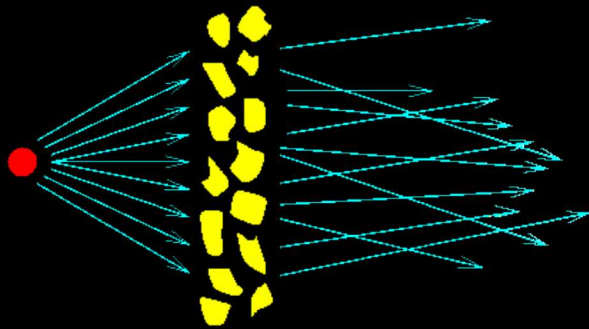
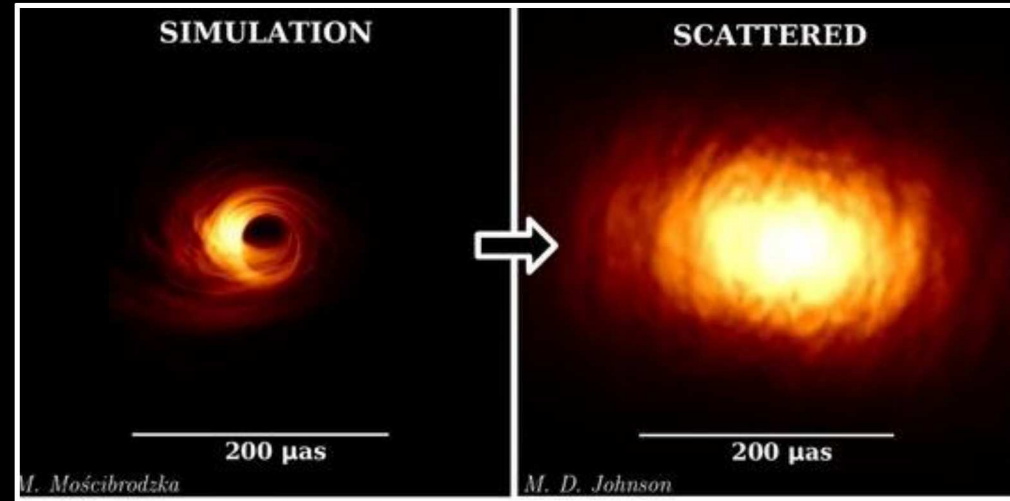
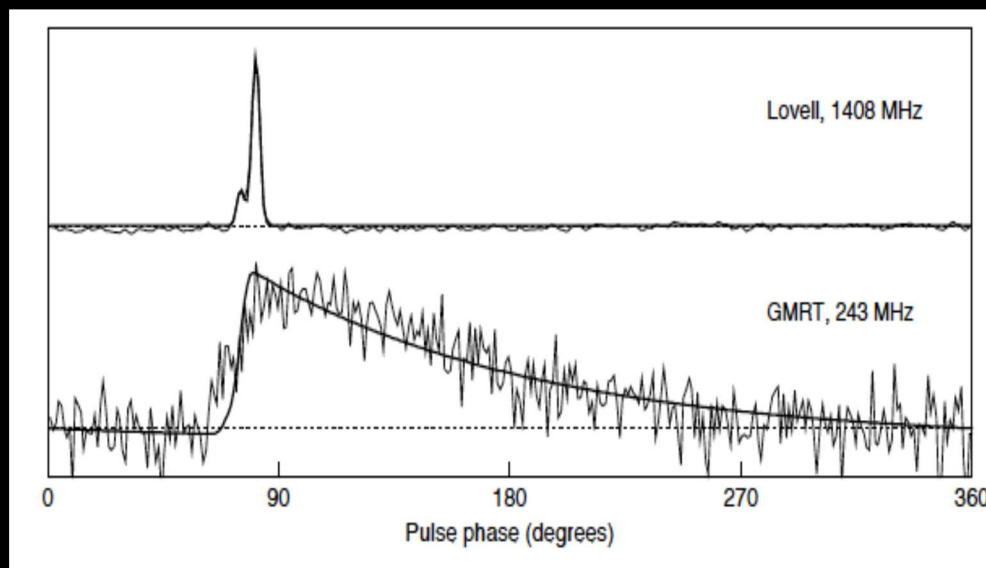


Image
Blur



Pulse
Smearing

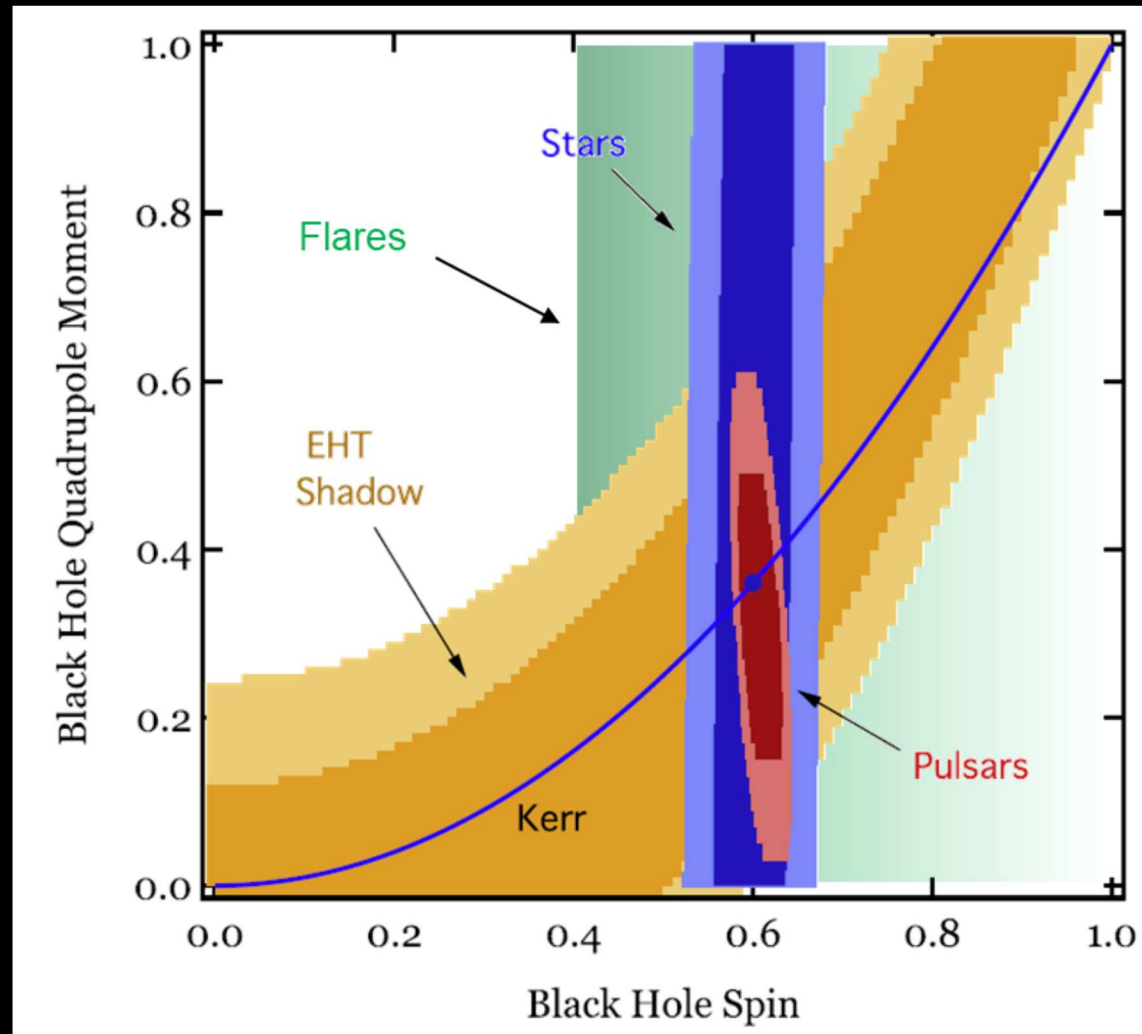


Difficult for Imaging
because of Atmosphere

Need for High Frequencies

Pulsars Get Very Faint

Key will be to Bring Together Hard, Independent Numbers



Thank You for Your Attention

General Relativity is **so far** the correct theory ?

The mass is concentrated **at least** within **3-5** Schwarzschild radii

